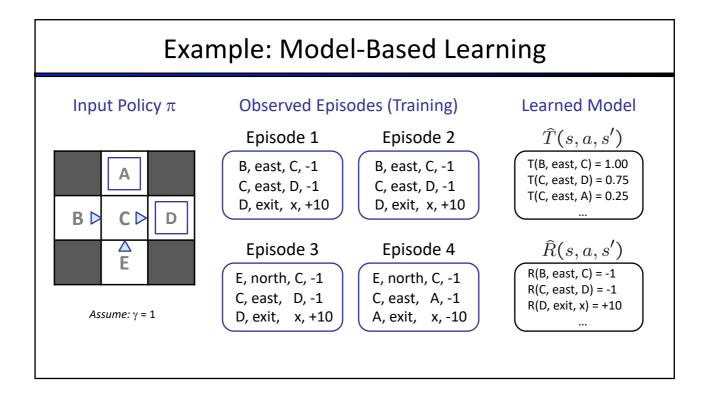
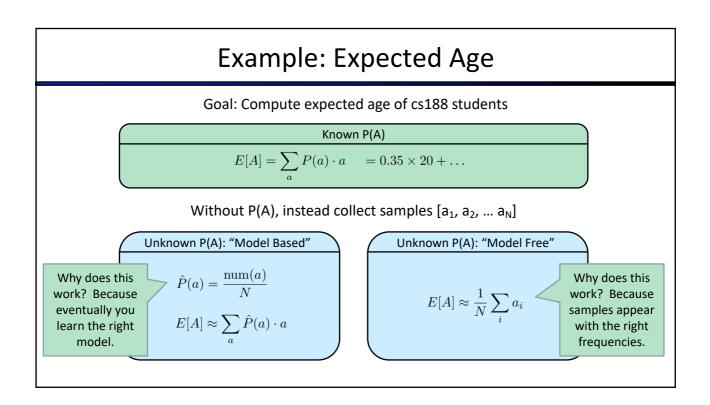
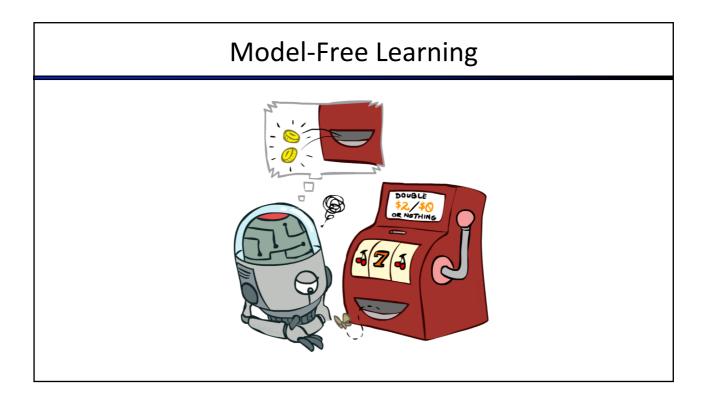
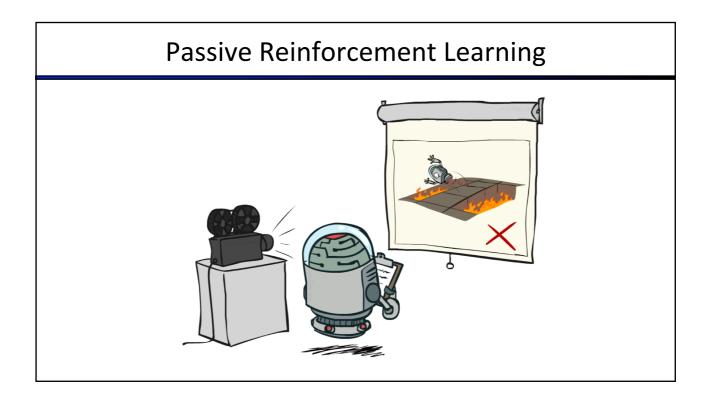


# <section-header> Model-Based Learning Model-Based Idea: Learn an approximate model based on experiences Solve for values as if the learned model were correct Step 1: Learn empirical MDP model Count outcomes s' for each s, a Normalize to give an estimate of Î(s, a, s') Discover each Â(s, a, s') when we experience (s, a, s') Step 2: Solve the learned MDP For example, use value iteration, as before









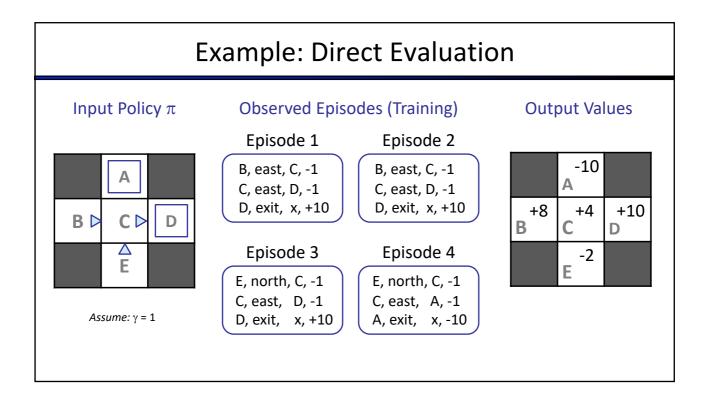
## Passive Reinforcement Learning

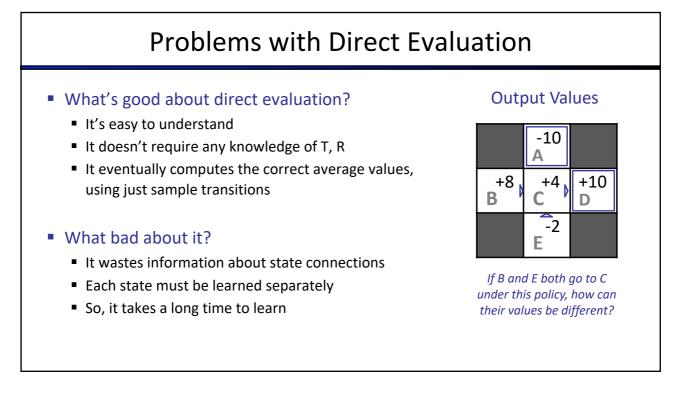
- Simplified task: policy evaluation
  - Input: a fixed policy π(s)
  - You don't know the transitions T(s,a,s')
  - You don't know the rewards R(s,a,s')
  - Goal: learn the state values
- In this case:
  - Learner is "along for the ride"
  - No choice about what actions to take
  - Just execute the policy and learn from experience
  - This is NOT offline planning! You actually take actions in the world.

## **Direct Evaluation**

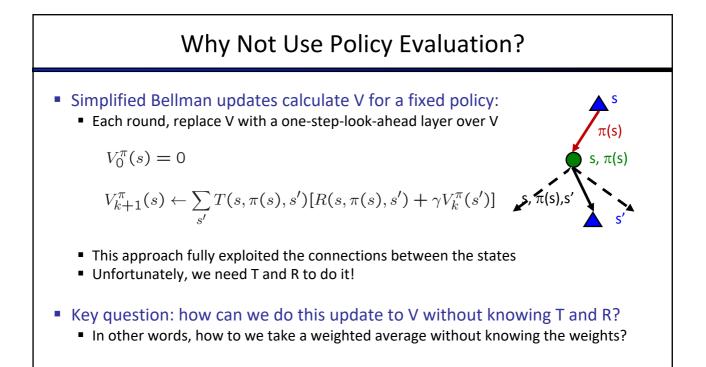
- Goal: Compute values for each state under π
- Idea: Average together observed sample values
  - Act according to  $\pi$
  - Every time you visit a state, write down what the sum of discounted rewards turned out to be
  - Average those samples
- This is called direct evaluation

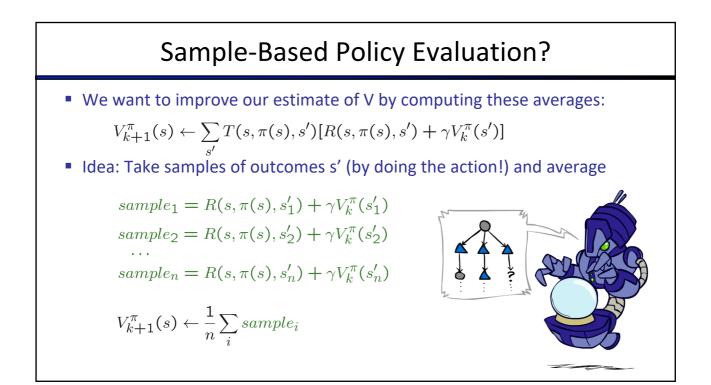




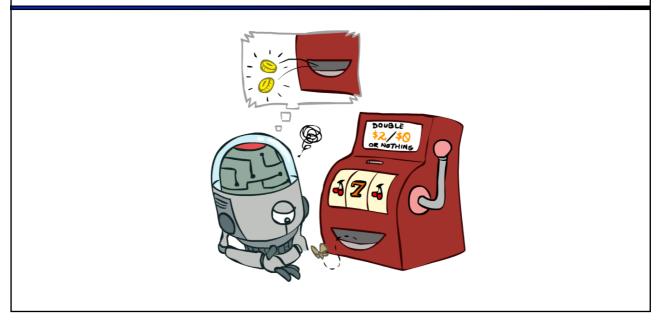


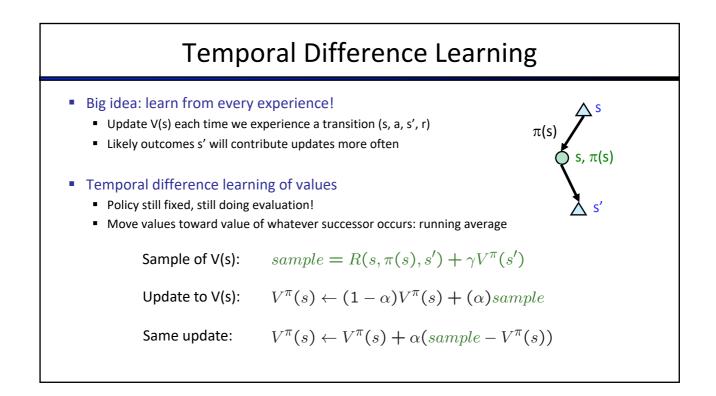
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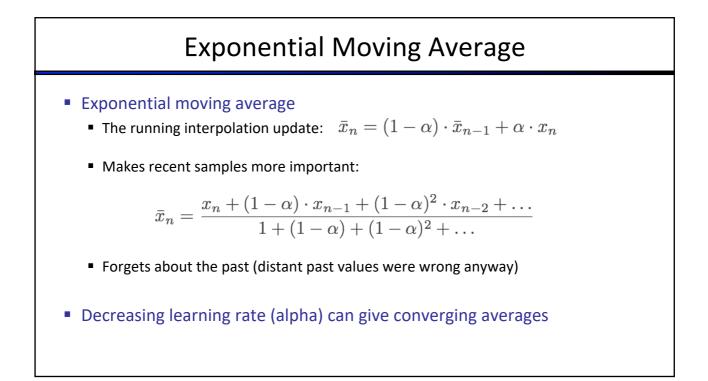


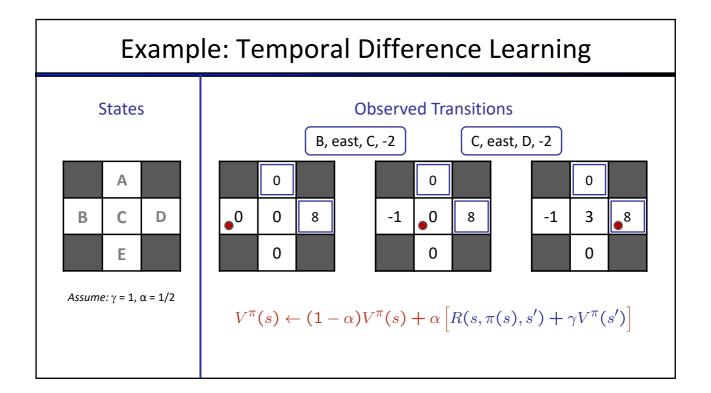


## **Temporal Difference Learning**







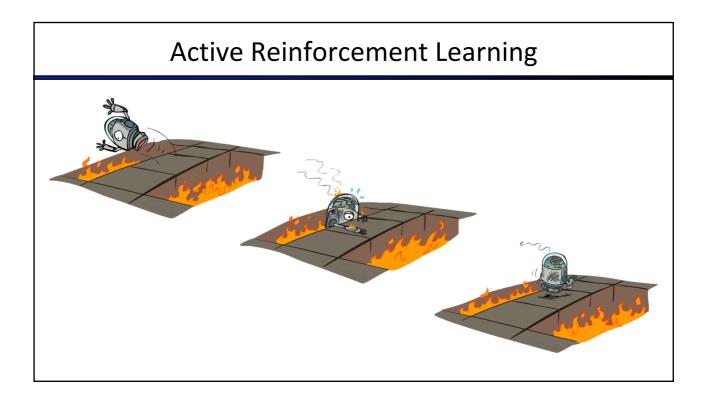


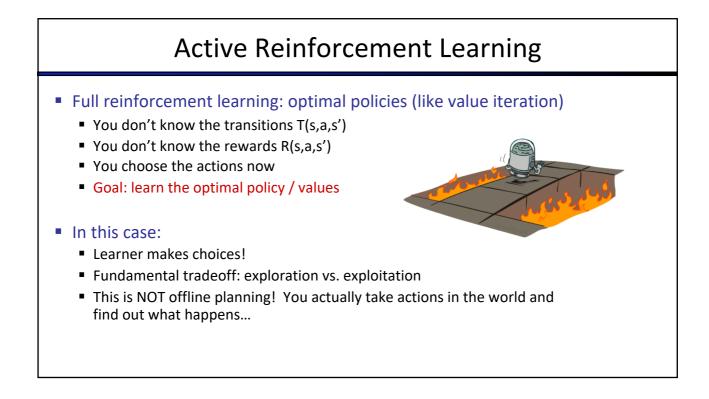
## Problems with TD Value Learning

- TD value leaning is a model-free way to do policy evaluation, mimicking Bellman updates with running sample averages
- However, if we want to turn values into a (new) policy, we're sunk:

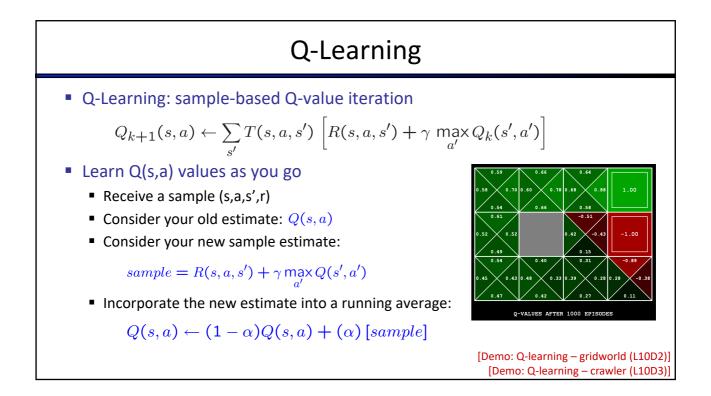
$$\pi(s) = \arg\max_{a} Q(s, a)$$
$$Q(s, a) = \sum_{s'} T(s, a, s') \left[ R(s, a, s') + \gamma V(s') \right]$$

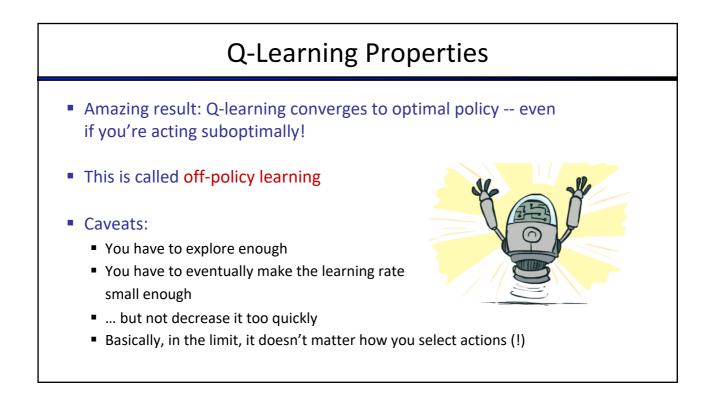
- Idea: learn Q-values, not values
- Makes action selection model-free too!

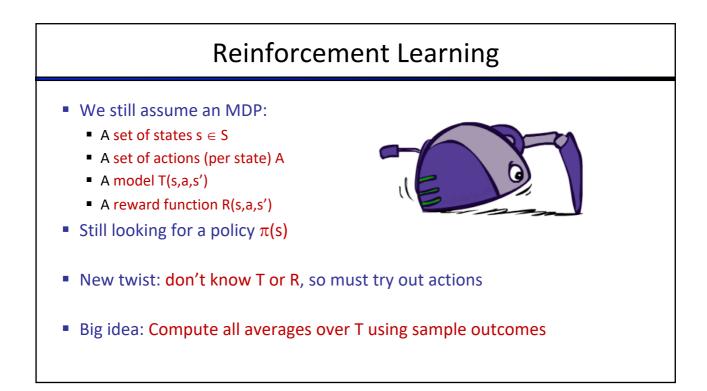




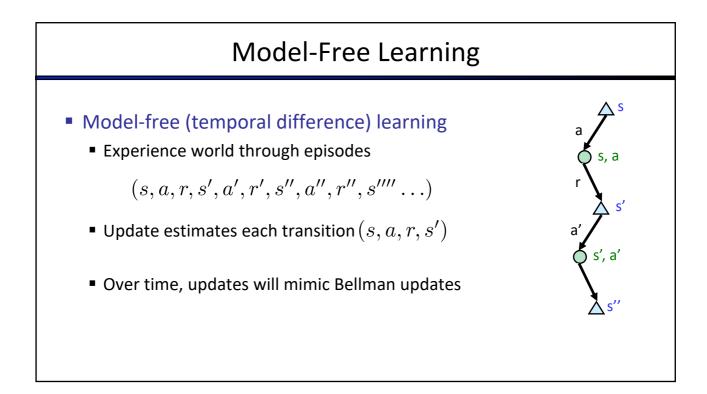
**Detour: Q-Value Iteration**  
**Value iteration: find successive (depth-limited) values**  
• Start with 
$$V_0(s) = 0$$
, which we know is right  
• Given  $V_{kr}$  calculate the depth k+1 values for all states:  
 $V_{k+1}(s) \leftarrow \max_{a} \sum_{s'} T(s, a, s') \left[ R(s, a, s') + \gamma V_k(s') \right]$   
• But Q-values are more useful, so compute them instead  
• Start with  $Q_0(s,a) = 0$ , which we know is right  
• Given  $Q_{kr}$  calculate the depth k+1 q-values for all q-states:  
 $Q_{k+1}(s, a) \leftarrow \sum_{s'} T(s, a, s') \left[ R(s, a, s') + \gamma \max_{a'} Q_k(s', a') \right]$ 

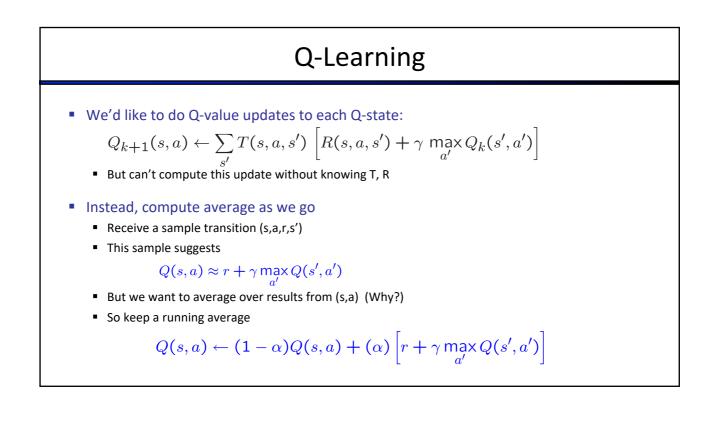


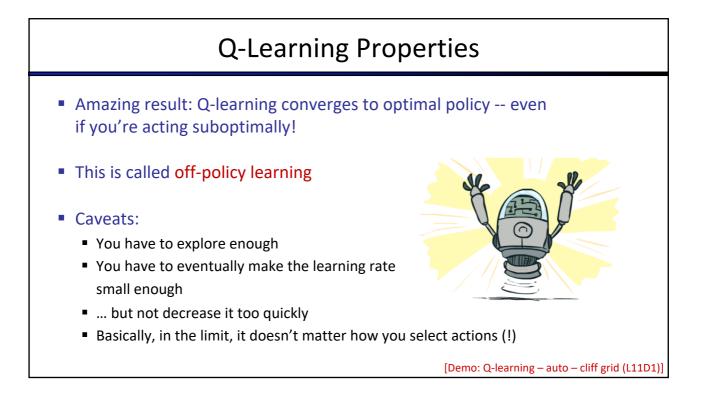


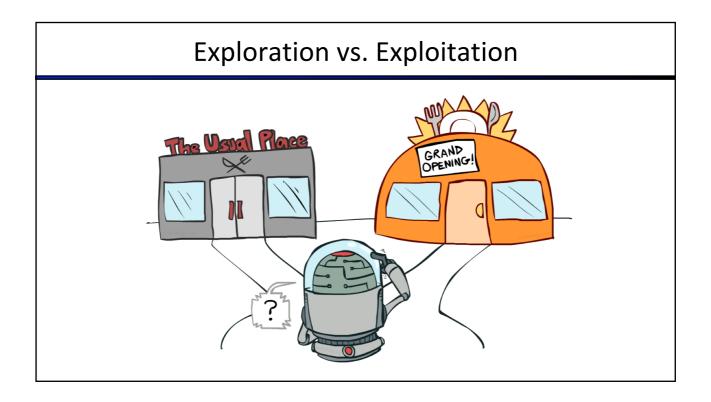


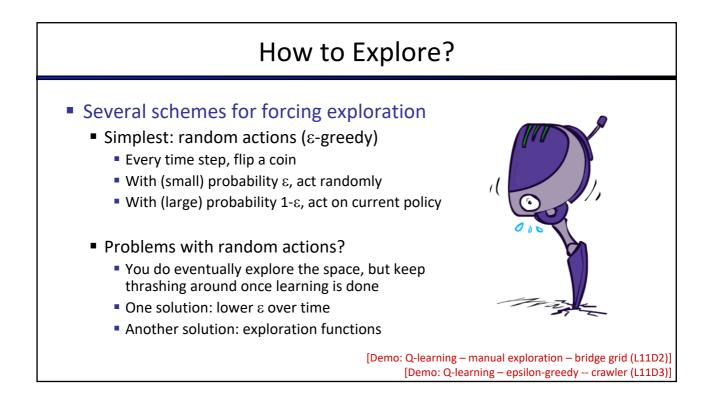
	Known MDP:	Offline Solution		
	Goal	Technique		
	Compute V*, Q*, $\pi^*$	Value / policy	Value / policy iteration	
	Evaluate a fixed policy $\boldsymbol{\pi}$	Policy evaluat	on	
Unknown MDP	: Model-Based	Unknowr	MDP: Model-Fr	ee
	: Model-Based Technique	Unknowr Goal	MDP: Model-Fro	ee
Unknown MDP Goal Compute V*, Q*, π*			Technique	ee

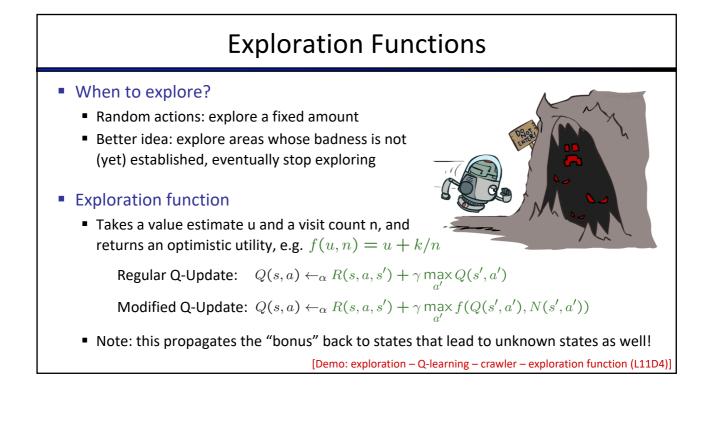




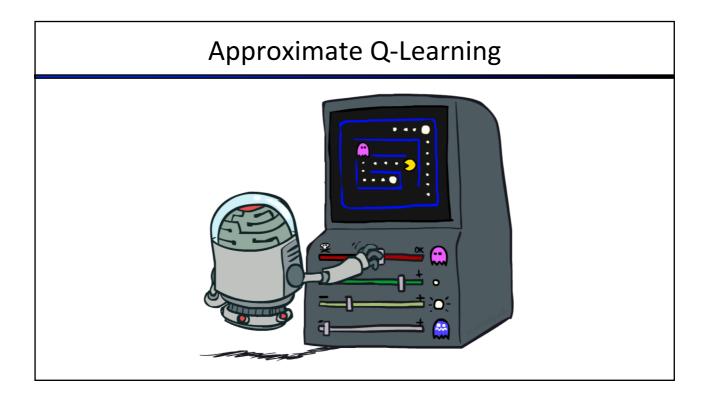


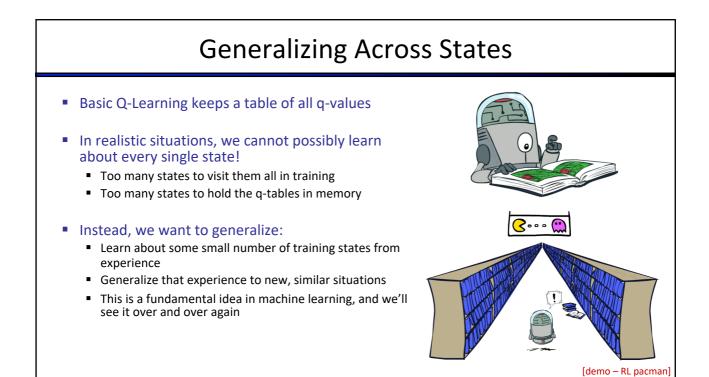


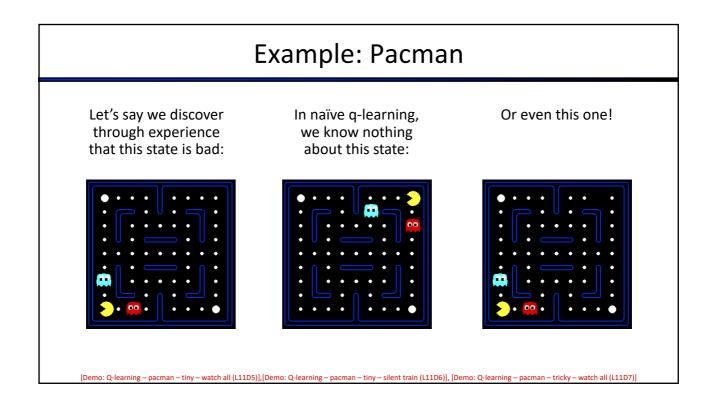


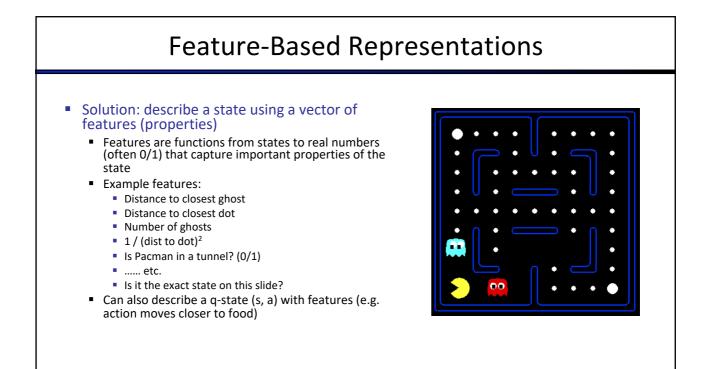


## Even if you learn the optimal policy, you still make mistakes along the way. Regret is a measure of your total mistake cost: the difference between your (expected) rewards, including youthful suboptimality, and optimal (expected) rewards. Minimizing regret goes beyond learning to be optimal – it requires optimally learning to be optimal. Example: random exploration and exploration functions both end up optimal, but random exploration has higher regret.









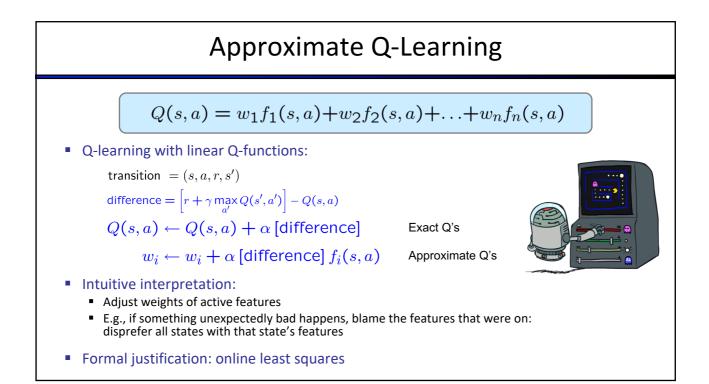
## **Linear Value Functions**

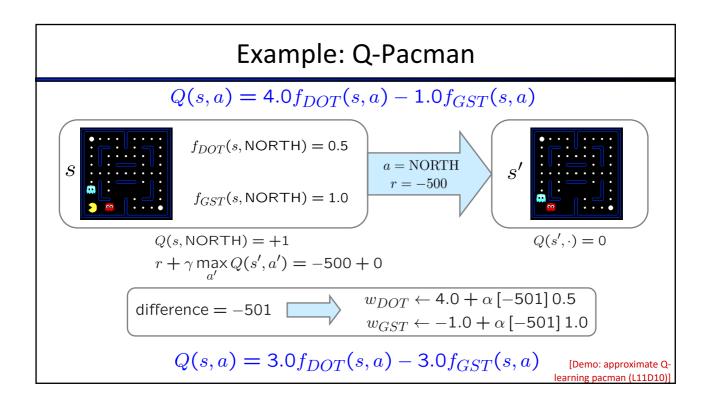
 Using a feature representation, we can write a q function (or value function) for any state using a few weights:

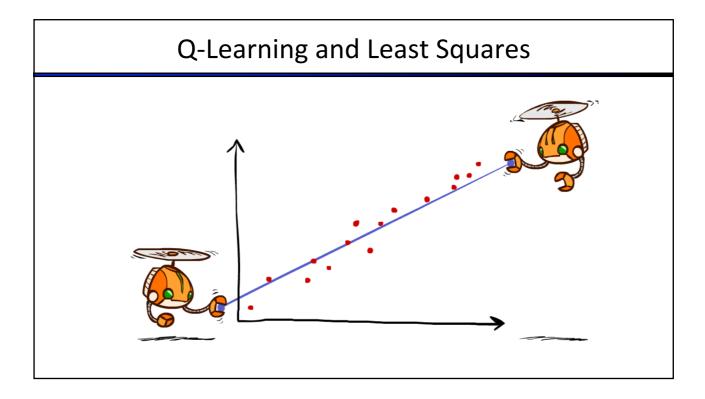
$$V(s) = w_1 f_1(s) + w_2 f_2(s) + \ldots + w_n f_n(s)$$

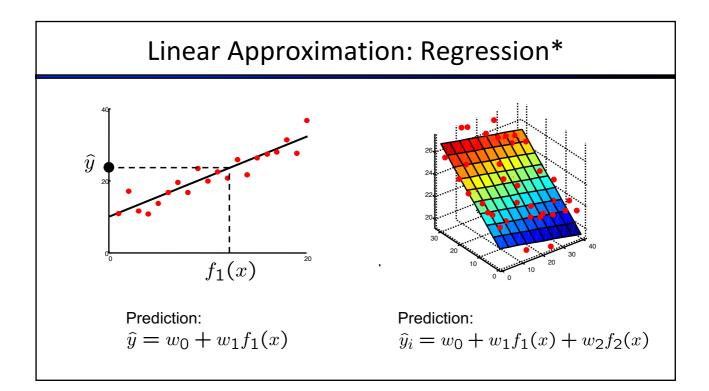
$$Q(s,a) = w_1 f_1(s,a) + w_2 f_2(s,a) + \ldots + w_n f_n(s,a)$$

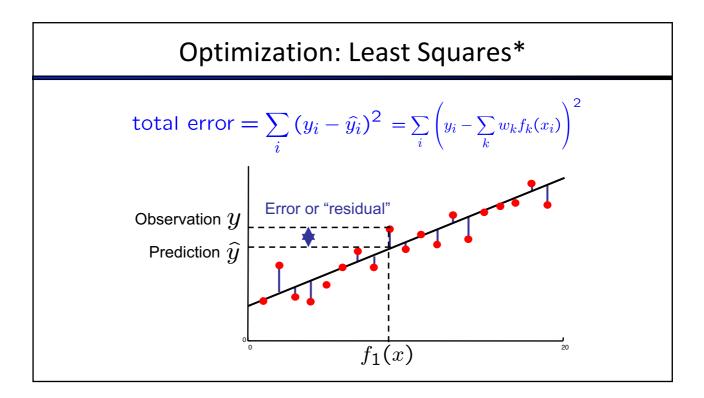
- Advantage: our experience is summed up in a few powerful numbers
- Disadvantage: states may share features but actually be very different in value!

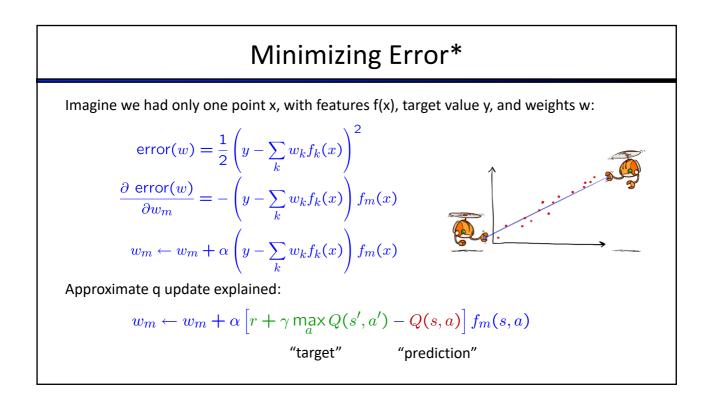


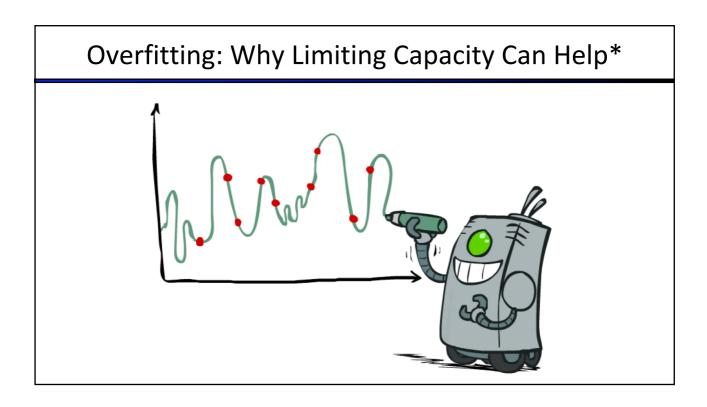


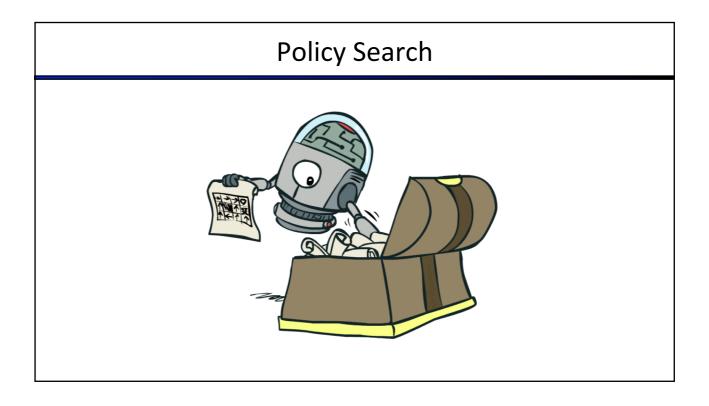












## Policy Search

- Problem: often the feature-based policies that work well (win games, maximize utilities) aren't the ones that approximate V / Q best
  - E.g. your value functions from project 2 were probably horrible estimates of future rewards, but they still produced good decisions
  - Q-learning's priority: get Q-values close (modeling)
  - Action selection priority: get ordering of Q-values right (prediction)
  - We'll see this distinction between modeling and prediction again later in the course
- Solution: learn policies that maximize rewards, not the values that predict them
- Policy search: start with an ok solution (e.g. Q-learning) then fine-tune by hill climbing on feature weights

## **Policy Search**

- Simplest policy search:
  - Start with an initial linear value function or Q-function
  - Nudge each feature weight up and down and see if your policy is better than before

### Problems:

- How do we tell the policy got better?
- Need to run many sample episodes!
- If there are a lot of features, this can be impractical
- Better methods exploit lookahead structure, sample wisely, change multiple parameters...



