







## Image segmentation by thresholding

• But if the objects and background occupy different ranges of gray levels, we can "mark" the object pixels by a process called **thresholding**:

- Let F(i,j) be the original, gray level image
- B(i,j) is a **binary image** (pixels are either 0 or 1) created by **thresholding** F(i,j)
  - B(i,j) = 1 if F(i,j) < †
  - B(i,j) = 0 if F(i,j) >= t
  - We will assume that the 1's are the object pixels and the 0's are the background pixels

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## Histogram

Histogram - frequency gray-level -> empirical distribution of the intensity values h[i] - number of pixels of intensity i

Histogram equalization - making histogram flat

Passing the image through look-up table of the form of cumulative distribution function

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## Thresholding

Hand selection

- select a threshold by hand at the beginning of the day
- use that threshold all day long!
- Many threshold selection methods in the literature
  - Probabilistic methods
    - make parametric assumptions about object and background intensity distributions and then derive "optimal" thresholds
  - Structural methods

    - · Evaluate a range of thresholds wrt properties of resulting binary images
      - one with straightest edges, most easily
      - recognized objects, etc.
  - Local thresholding
    - apply thresholding methods to image windows

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An advanced probabilistic threshold selection method - minimizing Kullback information distance

- Suppose the observed histogram, f, is a mixture of the gray levels of the pixels from the object(s) and the pixels from the background
  - in an ideal world the histogram would contain just two spikes (this depends of the class of images/objects)
  - but
    - measurement noise
    - model noise (e.g., variations in ink density within a character)
    - edge blur (misalignment of object boundaries with pixel boundaries and optical imperfections of camera)

spread these spikes out into hills

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#### Kullback information distance

- Now, if we hypothesize a threshold, t, then all of these unknown parameters can be approximated from the image histogram.
- Let f(g) be the observed and normalized histogram - f(g) = percentage of pixels from image having gray level g

$$p_{o}(t) = \sum_{g=0}^{t} f(g) \qquad p_{b}(t) = 1 - p_{0}(t)$$
$$\mu_{o}(t) = \sum_{g=0}^{t} f(g)g \qquad \mu_{b}(t) = \sum_{g=t+1}^{\max} f(g)g$$



 So, for any hypothesized t, we can "predict" what the total normalized image histogram should be if our model (mixture of two Gaussians) is correct.

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$$P_{t}(g) = p_{o}f_{o}(g) + p_{b}f_{b}(g)$$

- The total normalized image histogram is **observed to be** f(g)
- So, the question reduces to:
- determine a suitable way to measure the similarity of P and f
- then search for the t that gives the highest similarity

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# Kullback information distance

• A suitable similarity measure is the Kullback directed divergence, defined as

$$K(t) = \sum_{g=0}^{\max} f(g) \log[\frac{f(g)}{P_t(g)}]$$

If  $P_t$  matches f exactly, then each term of the sum is 0 and K(t) takes on its minimal value of 0

• Gray levels where  $P_t$  and f disagree are penalized by the log term, weighted by the importance of that gray level (f(g))

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