

Show all work clearly and in order. Justify your answers whenever possible; You have 20 minutes to take this 10 point quiz.

**1.** (5 points) Provide asymptotic notation ( $O, \Theta, \Omega$ ) to the following functions (please use  $\Theta$  whenever possible),

1.  $50n \in \_\_(\sqrt{n})$

2.  $n! \in \_\_(n^n)$

3.  $\log n^5 \in \_\_(\log 10^n)$

4.  $(3n)! \in \_\_((10n)!)$

5.  $4.999^n \in \_\_(5^n)$

**2.** (2 points) What is  $5^{123} \bmod 124$ ? Please show steps of how you get the answer.

**3.** (3 points) What is  $\gcd(48, 7^{100})$ ? Please show steps of how you get the answer.