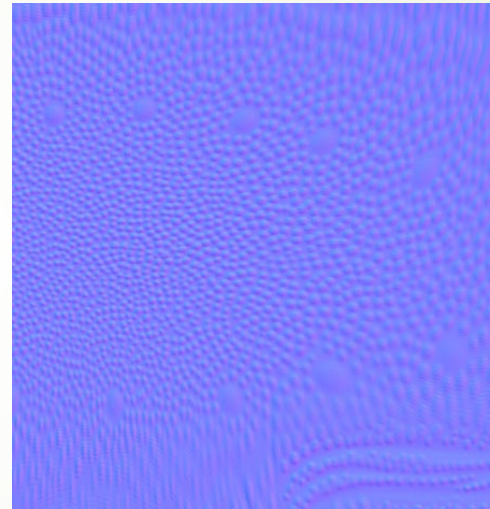


# CS451

## Texturing 4

Bump mapping continued



1

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# Spaces where your Normal map lives

- ▶ World space normal map
  - ▶ Each normal direction stored in texel is a world space vector
  - ▶ Usually applied to object using cube mapping
  - ▶ Rarely used for things that move
- ▶ Object space normal map
  - ▶ Each normal direction stored in texel is a vector in the space of the model
  - ▶ Each vertex must have unique  $(u,v)$  coordinates
- ▶ Tangent space normal map
  - ▶ Allow reuse of a normal map texture across multiple parts of the model

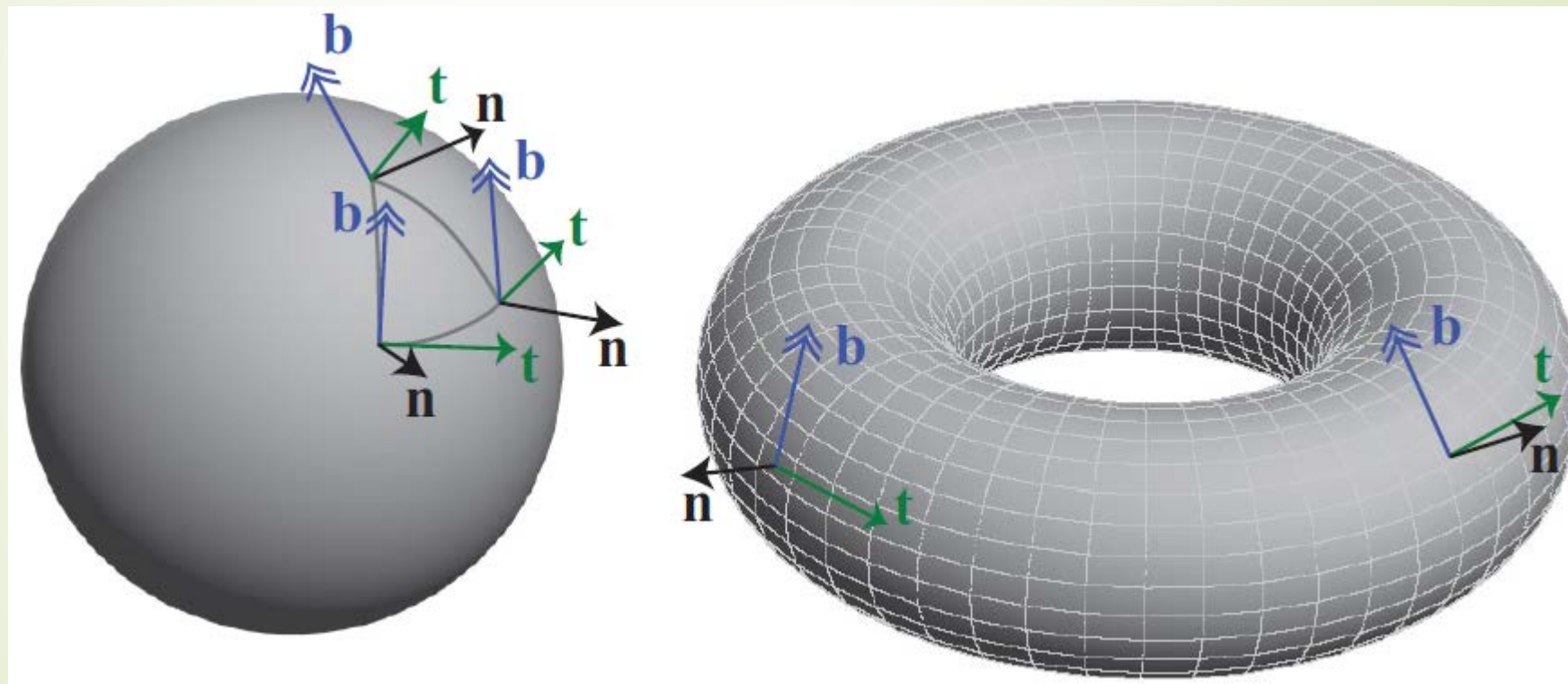
# Object-Space Normal Mapping

- ▶ 3d vector encoded
- ▶ Simpler to implement
- ▶ Reuse limited to
  - ▶ translation
  - ▶ Scaling
  - ▶ Rotation



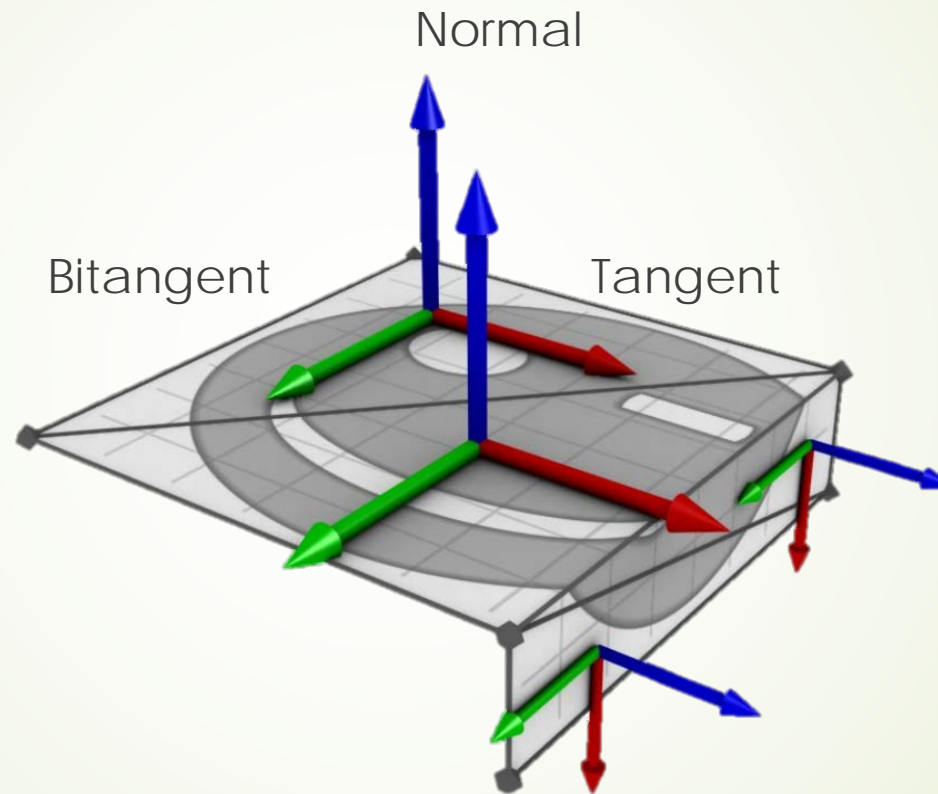
# Tangent Space

- Normal, tangent, Bi-tangent





# Tangent Space Per Triangle

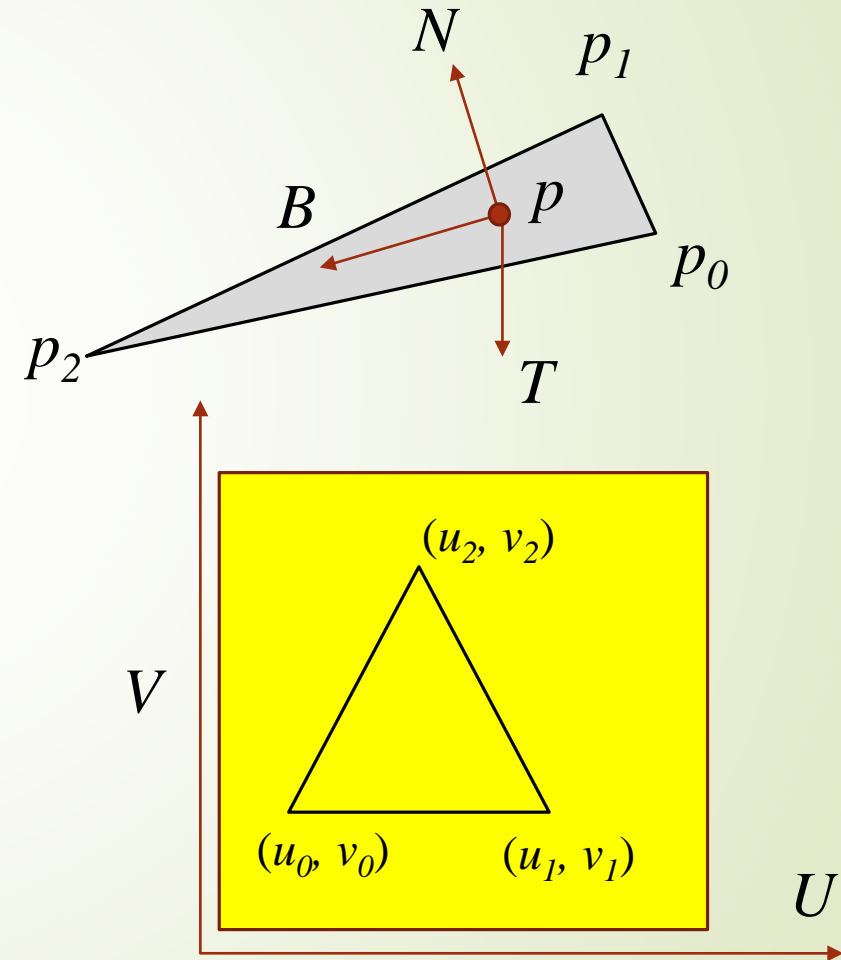


# How is Tangent Space Computed?

- ▶ Normal : perpendicular to the plane
- ▶ Tangent and bitangent are parallel to the plane
  - ▶ Tangent and bitangent are perpendicular to the normal
  - ▶ There are many possible tangents and bitangents
  - ▶ Their direction is determined by the UV coordinates
    - ▶ one points in the direction of U-axis in 3d space
    - ▶ the other in the direction of the V-axis
  - ▶ tangent space normal map stores the length of each vector

# How is Tangent Space Computed?

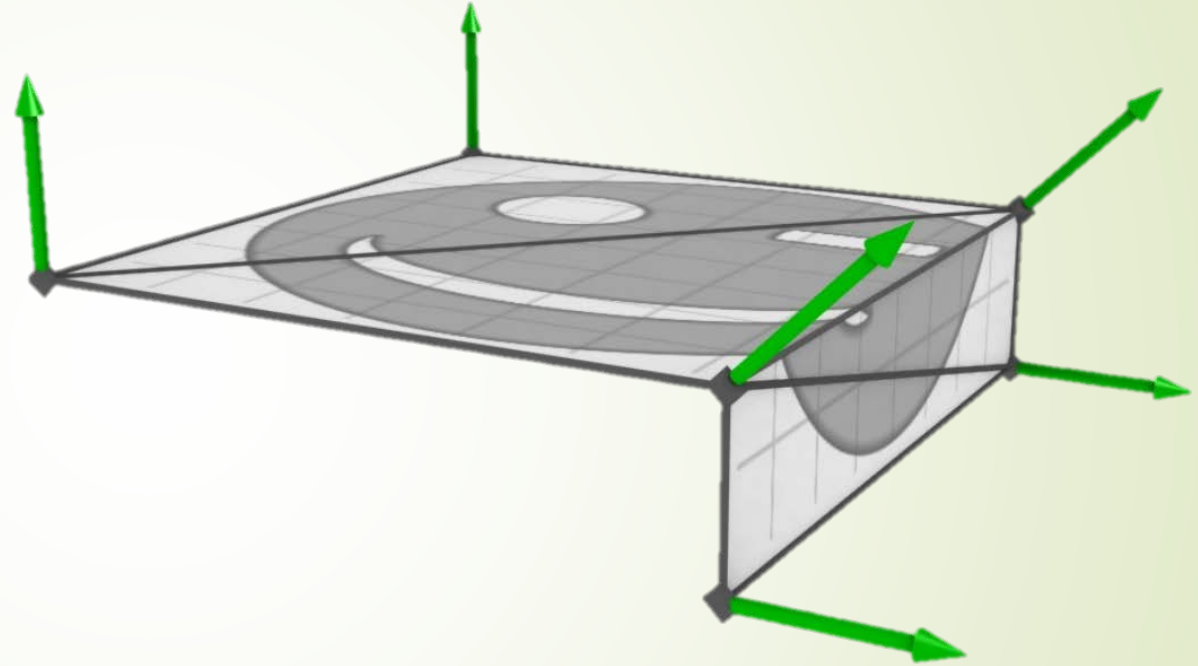
➤ Goal:  $P - P_0 = (u - u_0)T + (v - v_0)B$



Note:

$$\begin{bmatrix} s_1 & t_1 \\ s_2 & t_2 \end{bmatrix}^{-1} = \frac{1}{s_1 t_2 - s_2 t_1} \begin{bmatrix} t_2 & -t_1 \\ -s_2 & s_1 \end{bmatrix}$$

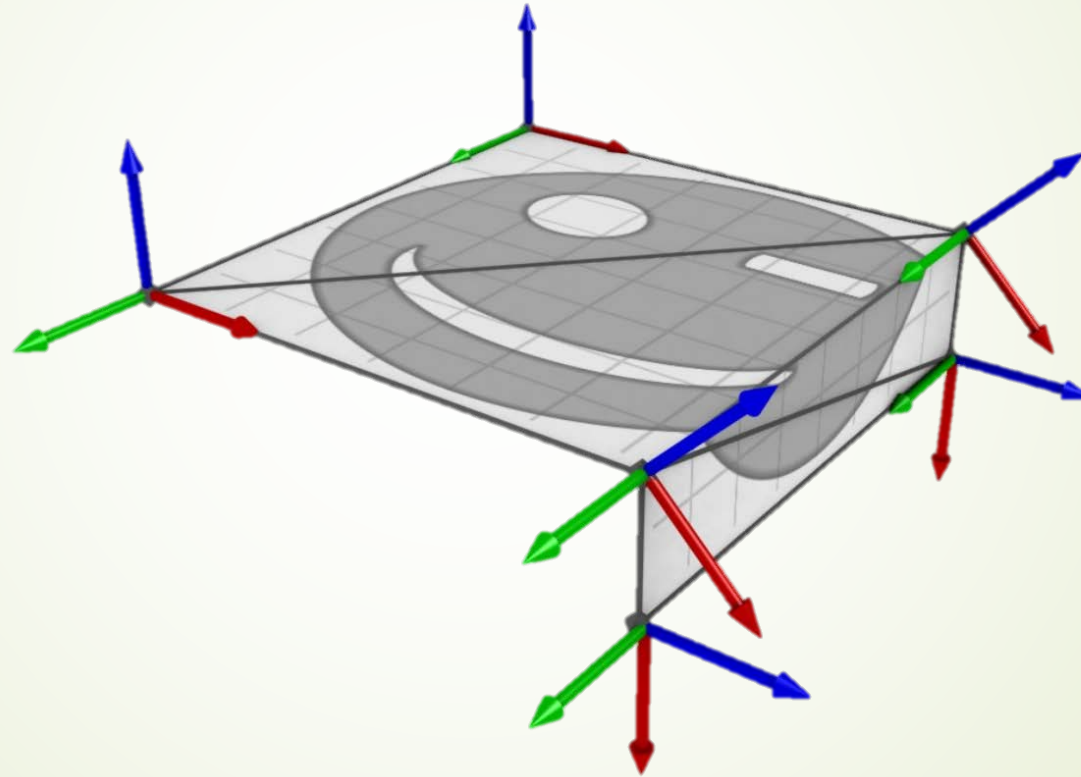
# Per Vertex Normal



- How do you compute per vertex normal?
- Is the normal affected by tessellation?



# Per Vertex Tangent Space



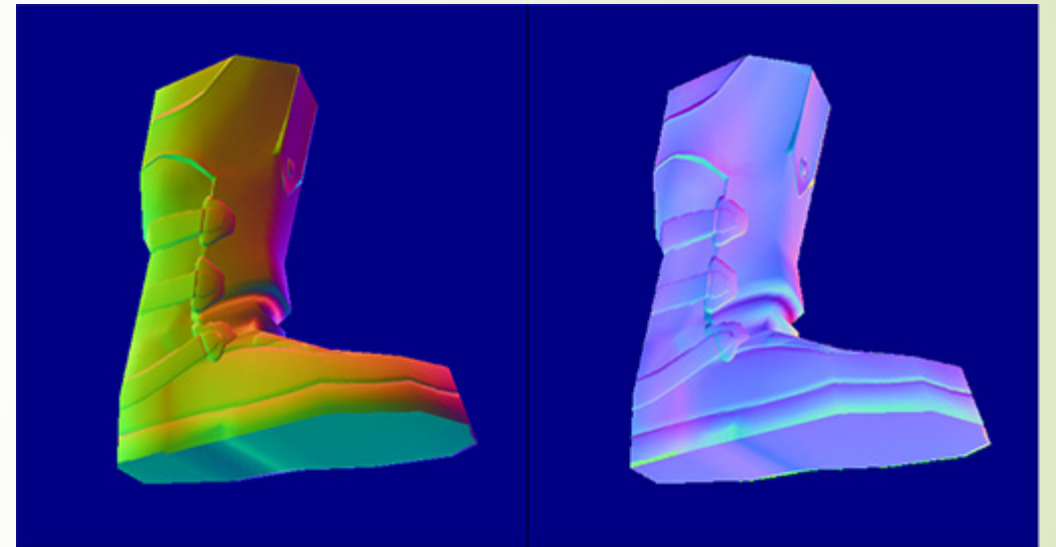
tangent space

$$\begin{bmatrix} T_1 & B_1 & N_1 \\ T_2 & B_2 & N_2 \\ T_3 & B_3 & N_3 \end{bmatrix}$$

How do you convert a light source to tangent space?

# Advantages of Tangent Space

- Efficient
- Support for mirroring
- Tiling textures
- Higher image compression rate

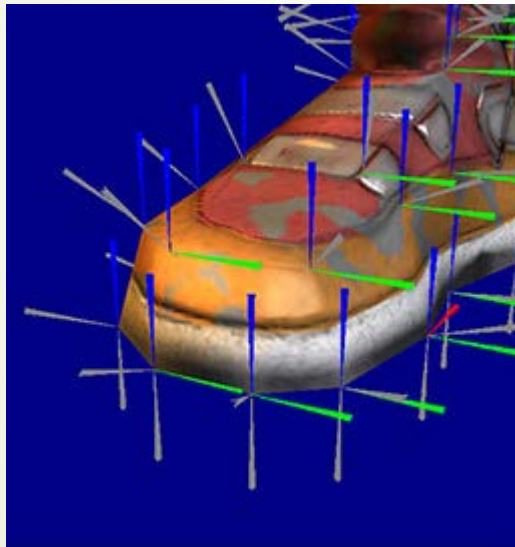


object space

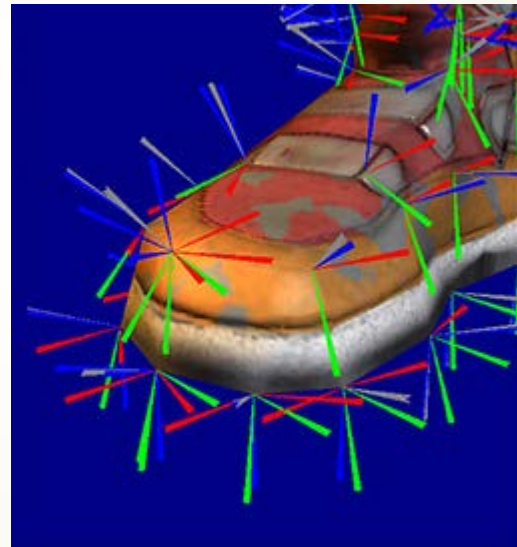
Tangent space

# Comparison

- ▶ The spaces defined by each vertex

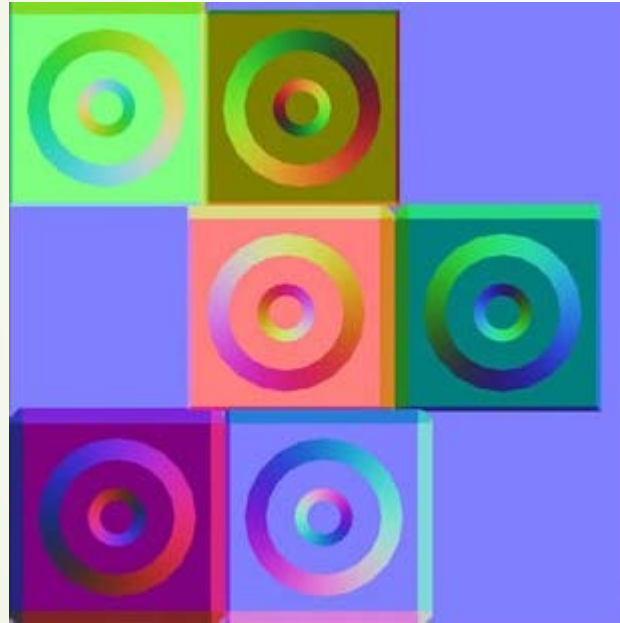
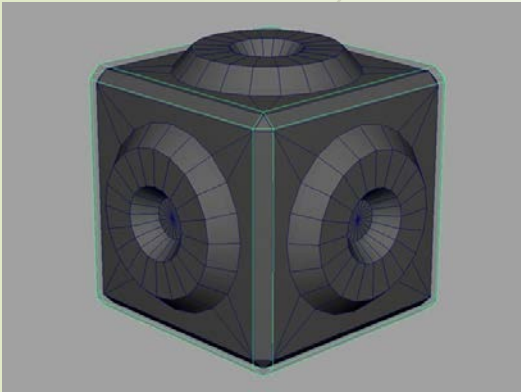


object space

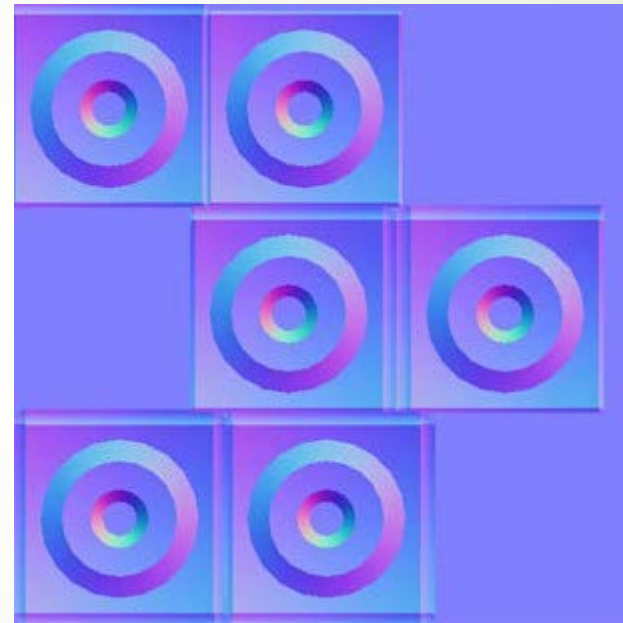


Tangent space

# Comparison



Object space



Tangent space



# What's Missing?

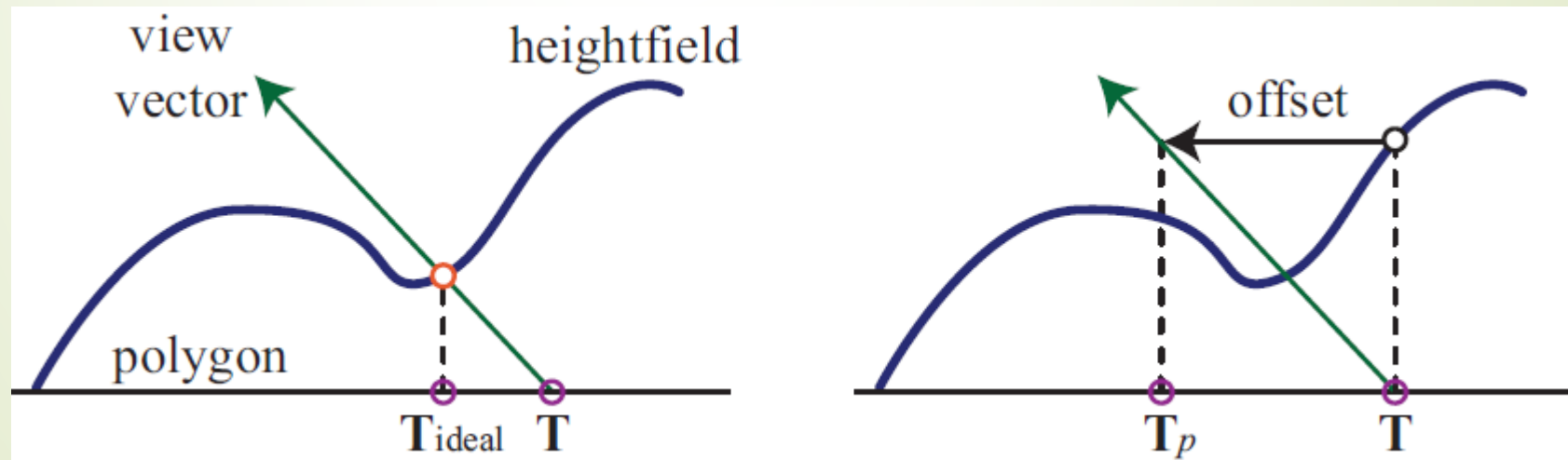
- ▶ There are no bumps on the silhouette of a bump-mapped object
- ▶ Bump maps don't allow self-occlusion or self-shadowing





# Parallax Mapping

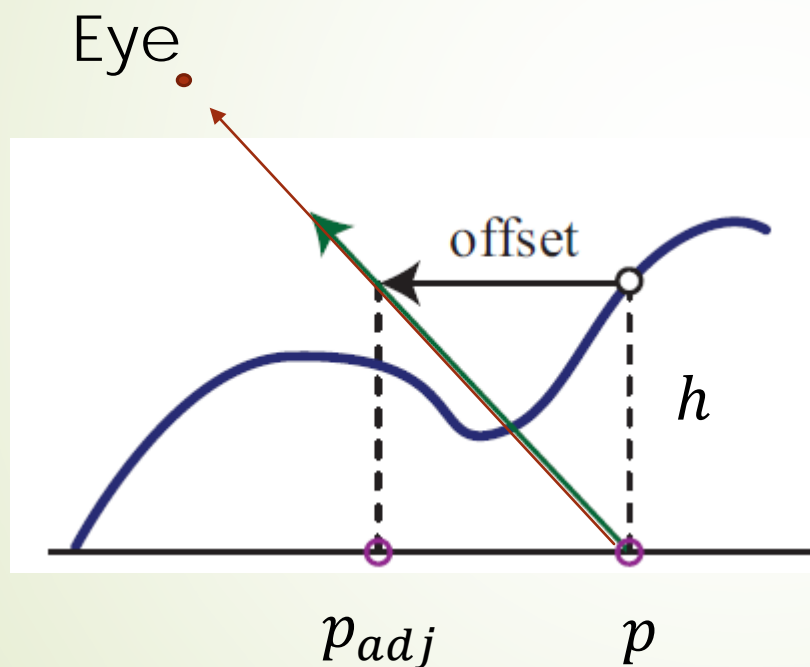
- A.k.a. Offset mapping, visual displacement mapping
- Using height field instead of normal map
- Example: What is the elevation and color for the green ray below



# Parallax Mapping

Vector from eye to  $p$

$$v = (v_x, v_y, v_z)$$

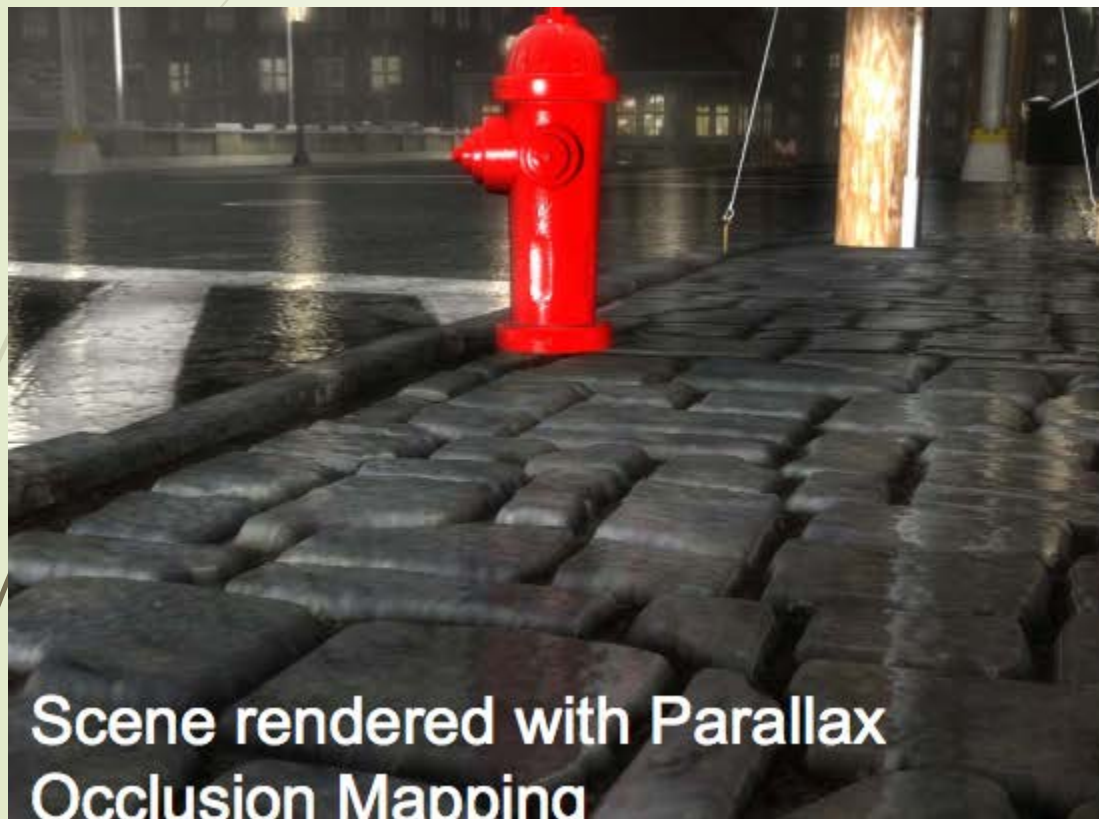


Solve  $p_{adj}$

Then the color of this ray is computed using color, normal defined at  $p_{adj}$  instead of those at  $p$

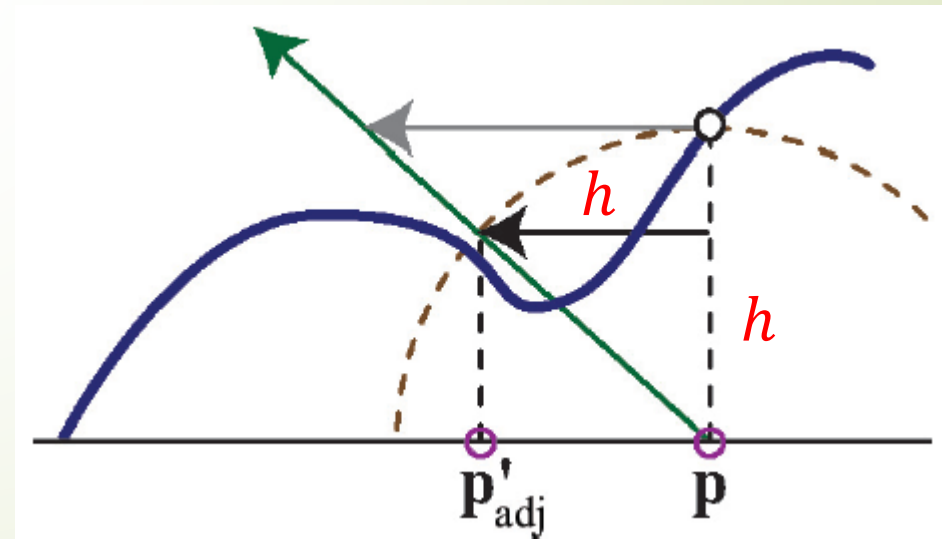
# Parallax Mapping

- ▶ Parallax provides much better visualization of "occlusion"



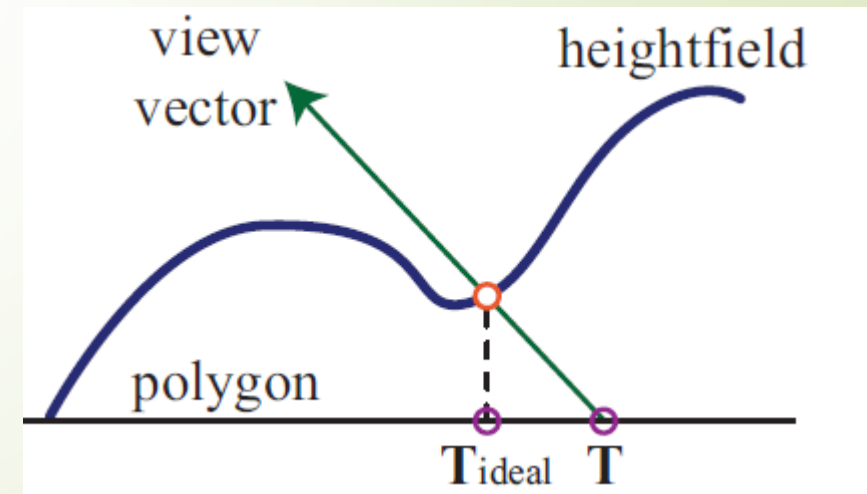
# Parallax Offset Limiting

- ▶ Parallax fails if the neighboring heights are very different
- ▶ Solution: limit the amount of offset
- ▶  $p'_{adj} = p + h \cdot v_{xy}$



# Relief Mapping

- Relief mapping (a.k.a. Steep parallax mapping or parallax occlusion mapping)
- Compute the first intersection between the ray and the height field **via Sampling**
- Still an approximation



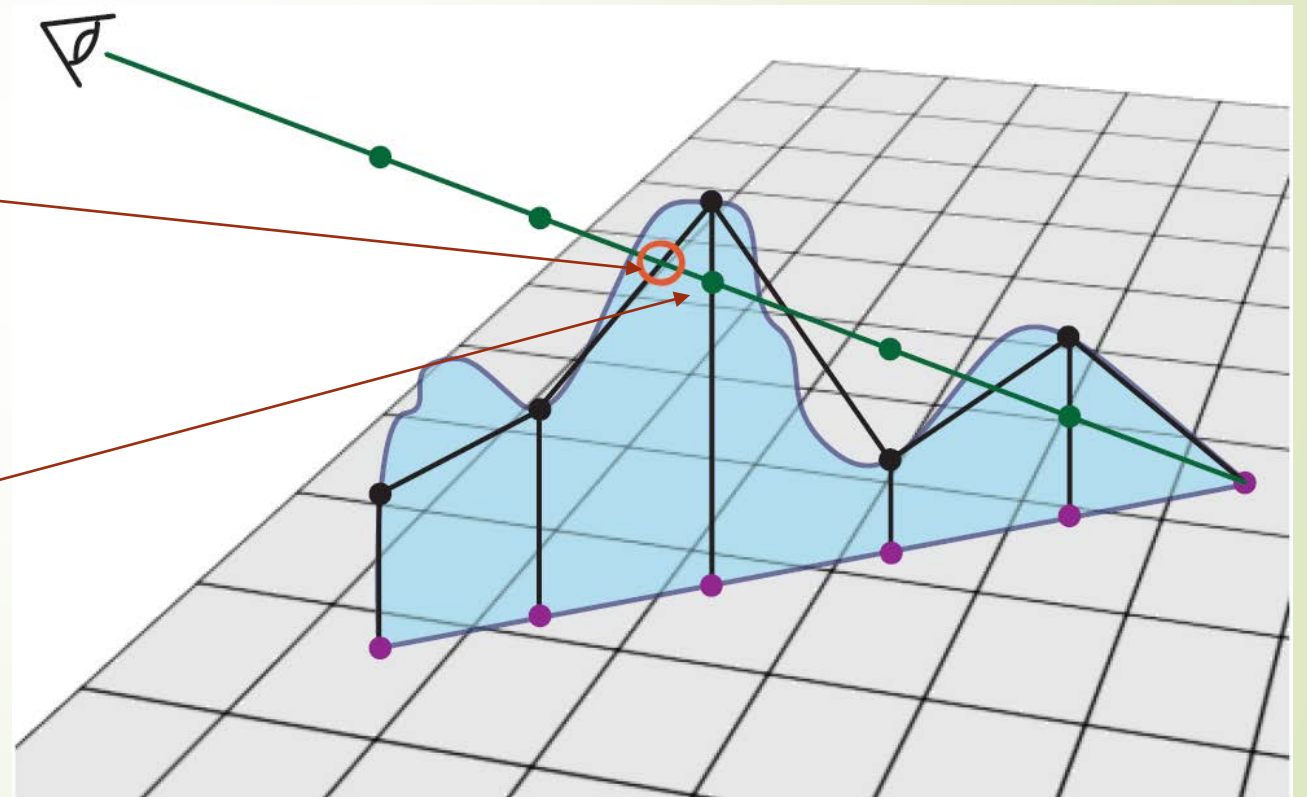


# Relief Mapping

- Sample along the viewing ray

**Goal:** compute this point

First sample lower than the height map





# Comparison



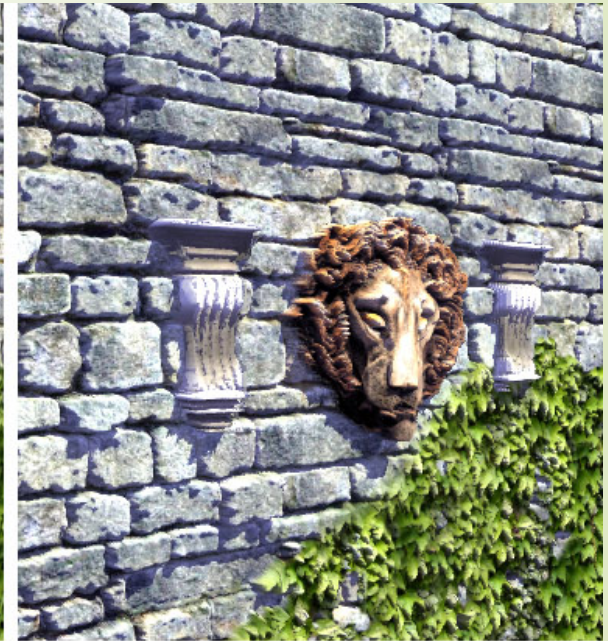
Texture Mapped



Normal Mapped



Parallax Mapped



Steep Parallax Mapped





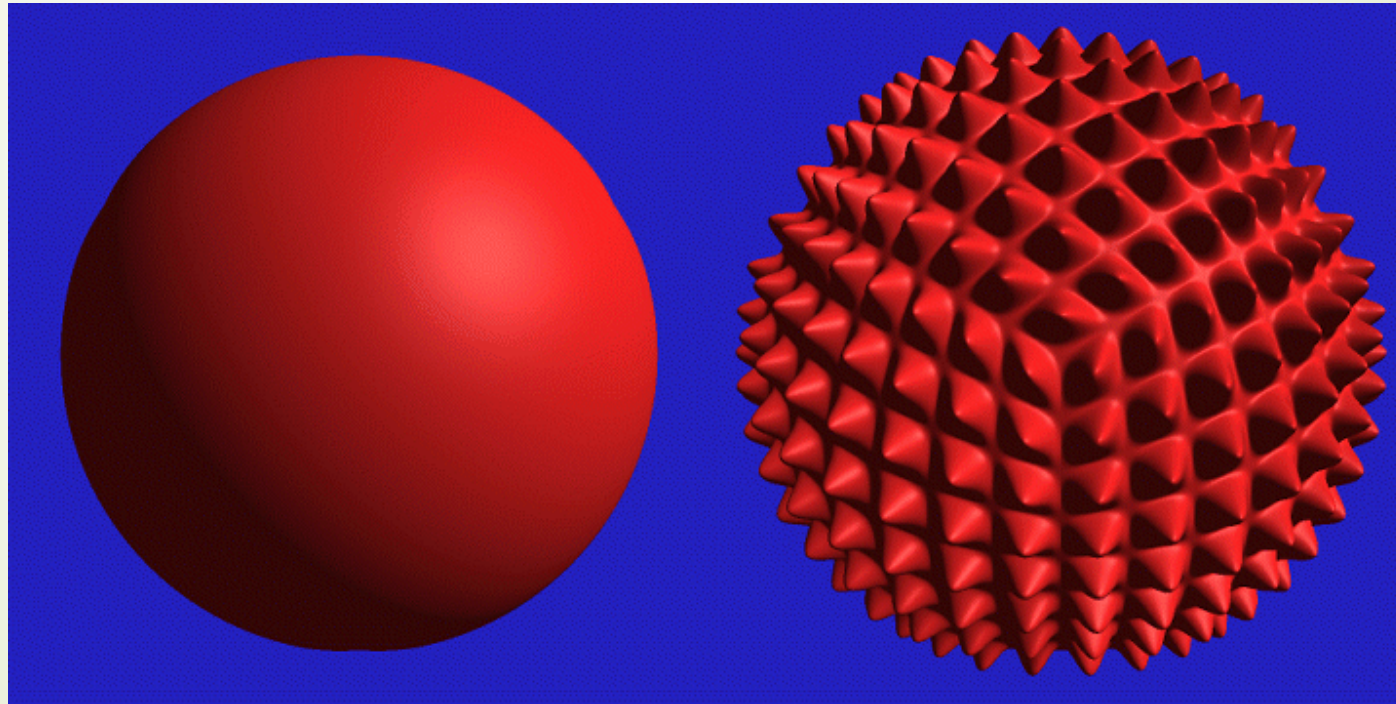
Great visual effect



Not so much if the  
silhouette is revealed

# Displacement Mapping

- ▶ Use the texture map to actually move the surface point
- ▶ The geometry must be displaced before visibility is determined





# Displacement Mapping



Image from:

*Geometry Caching for  
Ray-Tracing Displacement Maps*

by Matt Pharr and Pat Hanrahan.

*note the detailed shadows  
cast by the stones*



# Displacement Mapping



By Ken Musgrave

# Summary

- ▶ **Bump** mapping (using normal map, or height field)
  - ▶ Pro: Provide the illusion of local wrinkles
  - ▶ Con: No self-occlusion
- ▶ **Parallax** mapping
  - ▶ Pro: Provide self-occlusion
  - ▶ Con: The elevation cannot vary too much
- ▶ **Relief** mapping
  - ▶ Pro: Works with varying heights, can even provides shadow
  - ▶ Con: Bad visual effect on the silhouette
- ▶ **Displacement** mapping
  - ▶ Pro: bumps on silhouette
  - ▶ Con: Consume much more resources (CPU, GPU, memory)