

Intro to Software Testing

Chapter 8.1.4 & 8.1.5

Logic Coverage

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SWE 437

Adapted from slides by Paul Ammann & Jeff Offutt

Active Clauses

Determination

Clause **c_i determines** the value of its predicate when the other clauses have certain values

If **c_i** is changed, the value of the predicate changes

c_i is called the *major clause*

Other clauses are *minor clauses*

This is called ***making the clause active***

Determining Predicates

$$P = A \vee B$$

if **$B = \text{true}$** , p is always true.

so if **$B = \text{false}$** , A determines p .

if **$A = \text{false}$** , B determines p .

$$P = A \wedge B$$

if **$B = \text{false}$** , p is always false.

so if **$B = \text{true}$** , A determines p .

if **$A = \text{true}$** , B determines p .

- **Goal** : Find tests for each clause when the clause determines the value of the predicate

Infeasibility & Subsumption (8.1.4)

Consider the predicate:

$$(a > b \wedge b > c)$$

Realize the *abstract* test *tt* into a *concrete* test by finding values for *a*, *b*, and *c* that create the truth assignments *tt*

$$a=9, b=7, c=5$$

Now consider the predicate:

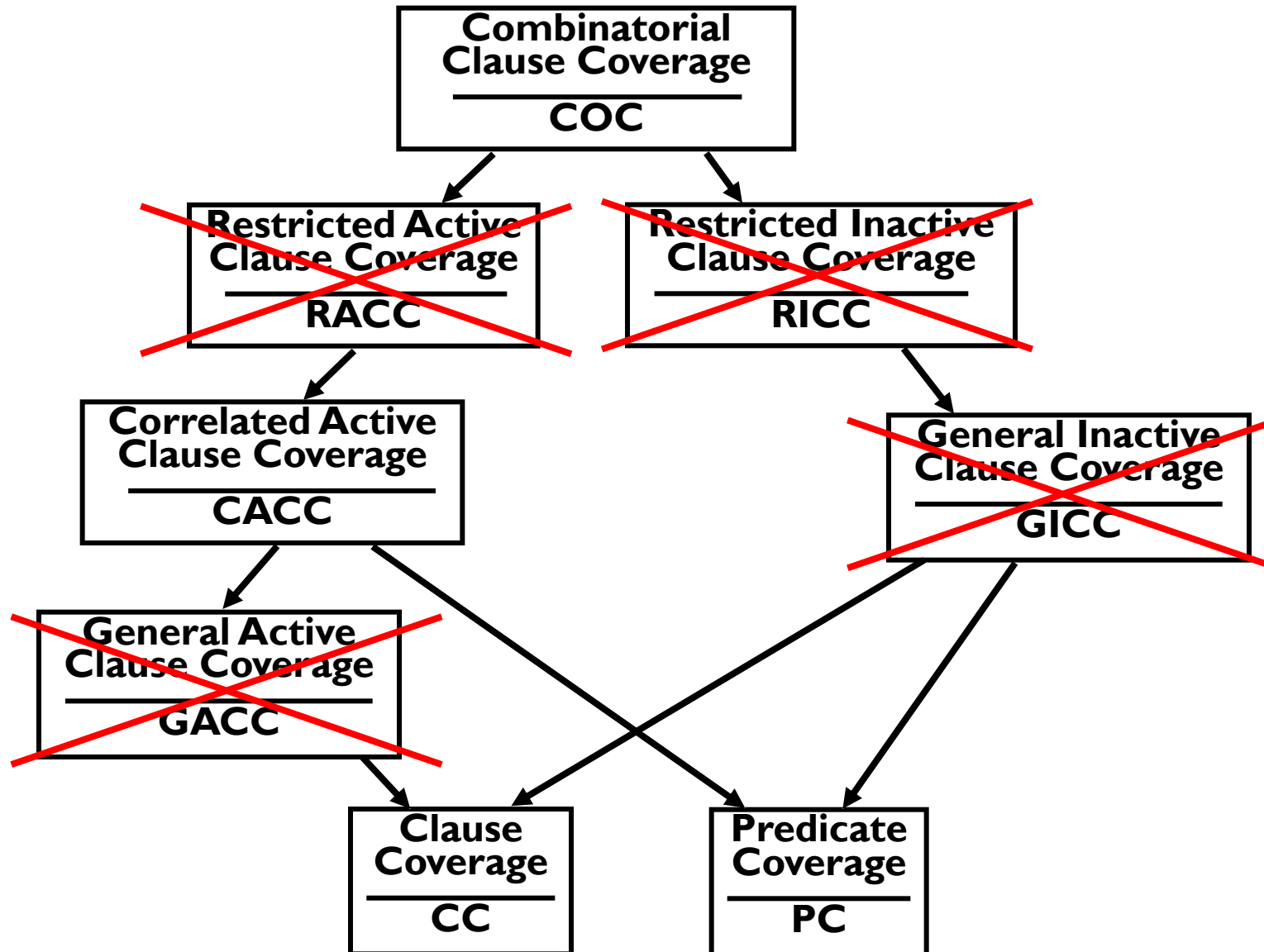
$$(a > b \wedge b > c) \vee c > a$$

Realize the *abstract* test *ttt* into a *concrete* test by finding values for *a*, *b*, and *c* that create the truth assignments *ttt*

Impossible!

- Infeasible test requirements are **recognized** and **ignored**
- Recognizing infeasible test requirements is generally **undecidable**
 - Thus usually done by hand

Logic Criteria Subsumption



Making Clauses Determine a Predicate

Three techniques

1. Informal **by inspection**

- This is what we've been doing
- Fast, but mistake-prone and does not scale—for experts

2. **Tabular** method





- Very simple by hand
- Few mistakes, slower, scales well to 5 or 6 clauses

3. **Definitional** method

- More mathematical
- Scales arbitrarily

Tabular Method

Find pairs of rows in the truth table

	a	b	$P=a \wedge b$	p_a	p_b
1	T	T	T		
2	T	F	F		
3	F	T	F		
4	F	F	F		

For p_a , find a **pair** of rows where





- **b is the same** in both
- **a is different**
- **P is different**

For p_b , find a **pair** of rows where

- **a is the same** in both
- **b is different**
- **P is different**

Tabular Method

Find pairs of rows in the truth table

	a	b	$P=a \wedge b$	p_a	p_b
1	T	T	T		
2	T	F	F		
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For P_a , find a **pair** of rows where

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- **a is different**
- **P is different**

For P_b , find a **pair** of rows where

- **a is the same** in both
- **b is different**
- **P is different**

Now do the same for "or"

	a	b	$P=a \vee b$	p_a	p_b
1	T	T	T		
2	T	F	T		
3	F	T	T		
4	F	F	F		

In-class Exercise

Tabular method

Use the tabular method to solve for P_a , P_b , and P_c .
Give solutions as pairs of rows.

	a	b	c	$a \wedge (b \vee c)$	P_a	P_b	P_c
1	T	T	T	T			
2	T	T	F	T			
3	T	F	T	T			
4	T	F	F	F			
5	F	T	T	F			
6	F	T	F	F			
7	F	F	T	F			
8	F	F	F	F			

In-class Exercise

Tabular method

b & *c* are the same, *a* differs, and *p* differs ... thus TTT and FTT cause *a* to determine the value of *p*

Again, *b* & *c* are the same, so TTF and FTF cause *a* to determine the value of *p*

Finally, this third pair, TFT and FFT, also cause *a* to determine the value of *p*

For clause *b*, only one pair, TTF and TFF cause *b* to determine the value of *p*

Likewise, for clause *c*, only one pair, TFT and TFF, cause *c* to determine the value of *p*

	a	b	c	$a \wedge (b \vee c)$	p_a	p_b	p_c
1	T	T	T	T			
2	T	T	F	T			
3	T	F	T	T			
4	T	F	F	F			
5	F	T	T	F			
6	F	T	F	F			
7	F	F	T	F			
8	F	F	F	F			

Three separate pairs of rows can cause *a* to determine the predicate.

Only one pair each for *b* and *c*.

Definitional Method

Scales better (more clauses), requires more math

Definitional approach:

- $p_{c=true}$ is predicate p with every occurrence of c replaced by $true$
- $p_{c=false}$ is predicate p with every occurrence of c replaced by $false$

To find values for the minor clauses, connect $p_{c=true}$ and $p_{c=false}$ with exclusive *OR*

$$p_c = p_{c=true} \oplus p_{c=false}$$

After solving, p_c describes exactly the values needed for c to determine p

Definitional Method Examples

$$\underline{p = a \vee b}$$

$$\begin{aligned} p_a &= p_{a=\text{true}} \oplus p_{a=\text{false}} \\ &= (\text{true} \vee b) \text{ XOR } (\text{false} \vee b) \\ &= \text{true XOR } b \\ &= !b \end{aligned}$$

$$\underline{p = a \wedge b}$$

Use the definitional approach to solve for Pa

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Use the definitional approach to solve for P_a

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Use the definitional approach to solve for P_a

$$\underline{p = a \vee (b \wedge c)}$$

Use the definitional approach to solve for P_a

Definitional Method Examples

$$\underline{p = a \vee b}$$

$$\begin{aligned} p_a &= p_{a=\text{true}} \oplus p_{a=\text{false}} \\ &= (\text{true} \vee b) \text{ XOR } (\text{false} \vee b) \\ &= \text{true XOR } b \\ &= !b \end{aligned}$$

$$\underline{p = a \wedge b}$$

$$\begin{aligned} p_a &= p_{a=\text{true}} \oplus p_{a=\text{false}} \\ &= (\text{true} \wedge b) \oplus (\text{false} \wedge b) \\ &= b \oplus \text{false} \\ &= b \end{aligned}$$

Use the definitional approach to solve for Pa

$$\underline{p = a \vee (b \wedge c)}$$

$$\begin{aligned} p_a &= p_{a=\text{true}} \oplus p_{a=\text{false}} \\ &= (\text{true} \vee (b \wedge c)) \oplus (\text{false} \vee (b \wedge c)) \\ &= \text{true} \oplus (b \wedge c) \\ &= !(b \wedge c) \\ &= !b \vee !c \end{aligned}$$

Use the definitional approach to solve for Pa

"NOT b \vee NOT c" means either b or c must be false

XOR Identity Rules

Exclusive-OR (*xor*, \oplus) means both cannot be true

That is, $A \text{ xor } B$ means

"A or B is true, but not both"

$$\begin{aligned} p &= A \oplus A \wedge b \\ &= A \wedge \neg b \end{aligned}$$

$$\begin{aligned} p &= A \oplus A \vee b \\ &= \neg A \wedge b \end{aligned}$$

with fewer symbols ...

$$\begin{aligned} p &= A \text{ xor } (A \text{ and } b) \\ &= A \text{ and } !b \end{aligned}$$

$$\begin{aligned} p &= A \text{ xor } (A \text{ or } b) \\ &= !A \text{ and } b \end{aligned}$$

Repeated Variables

The definitions in this chapter yield the same tests no matter how the predicate is expressed

$$(a \vee b) \wedge (c \vee b) == (a \wedge c) \vee b$$

$$(a \wedge b) \vee (b \wedge c) \vee (a \wedge c)$$

- Only has 8 possible tests, not 64

Use the simplest form of the predicate, and ignore contradictory truth table assignments

A More Subtle Example

$$\underline{p = (a \wedge b) \vee (a \wedge ! b)}$$

$$\begin{aligned} p_a &= p_{a=true} \oplus p_{a=false} \\ &= ((\text{true} \wedge b) \vee (\text{true} \wedge ! b)) \oplus ((\text{false} \wedge b) \vee (\text{false} \wedge ! b)) \\ &= (b \vee ! b) \oplus \text{false} \\ &= \text{true} \oplus \text{false} \\ &= \text{true} \end{aligned}$$

$$\underline{p = (a \wedge b) \vee (a \wedge \neg b)}$$

$$\begin{aligned} p_b &= p_{b=true} \oplus p_{b=false} \\ &= ((a \wedge \text{true}) \vee (a \wedge ! \text{true})) \oplus ((a \wedge \text{false}) \vee (a \wedge ! \text{false})) \\ &= (a \vee \text{false}) \oplus (\text{false} \vee a) \\ &= a \oplus a \\ &= \text{false} \end{aligned}$$

- **a** always determines the value of this predicate
- **b** never determines the value – **b** is **irrelevant** !

Logic Coverage Summary

Predicates are often **very simple**—in practice, most have less than 3 clauses

- In fact, most predicates only have one clause !
- With only clause, PC is enough
- With 2 or 3 clauses, CoC is practical
- Advantages of ACC and ICC criteria significant for large predicates
 - CoC is impractical for predicates with many clauses

Control software often has many complicated predicates, with lots of clauses

In-Class Exercise

Definitional method

$$P = (a \mid b) \& (a \mid c) \& d$$

Use the definitional method to solve for Pa

First step: $((T \mid b) \& (T \mid c) \& d) \text{ xor } ((F \mid b) \& (F \mid c) \& d)$

In-Class Exercise

Definitional method

$$P = (a \mid b) \& (a \mid c) \& d$$

Use the definitional method to solve for Pa

First step: $((T \mid b) \& (T \mid c) \& d) \text{ xor } ((F \mid b) \& (F \mid c) \& d)$

$$\begin{aligned} Pa &= ((T \mid b) \& (T \mid c) \& d) \text{ xor } ((F \mid b) \& (F \mid c) \& d) \\ &= (T \& T \& d) \text{ xor } (b \& c \& d) \\ &= d \text{ xor } (b \& c \& d) \end{aligned}$$

$$\begin{aligned} &\text{Using the identity: } A \text{ xor } (A \& b) == A \text{ and } !b \\ &= d \& !(b \& c) \\ &= d \& (!b \mid !c) \end{aligned}$$