

# Architecture and Parallel Computers

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CS 499: Spring 2016 GMU

# Logistics

Reading: Grama Ch 2 + 3

- ▶ Ch 2.3-5 is most important for Ch 2
- ▶ Ch 3 all

## Assignment 1

- ▶ Posted, due Thu 2/4
- ▶ Groups of 2 permitted
- ▶ Questions?
- ▶ Office hours Tue 3:30-5:30pm

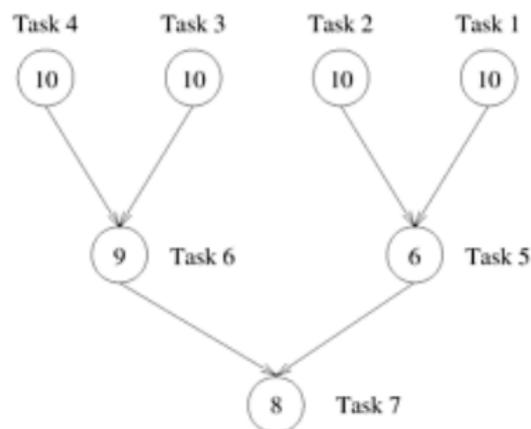
## Today

- ▶ Finish Parallel architecture (HW1: #1-2)
- ▶ Parallel Algorithm Decomposition (HW1: #3,4,6)

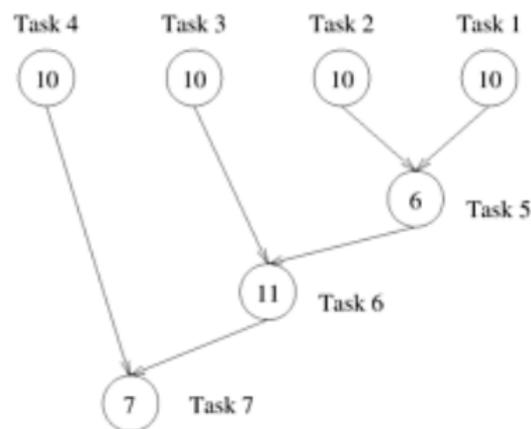
## Dependency Graphs

- ▶ Relation of tasks to one another
- ▶ Vertices: tasks, often labeled with time to complete
- ▶ Edges: indicate what must happen first
- ▶ Should be a DAG, Directed Acyclic Graph  
(If not, you're in trouble)

## Features of Dependency Graphs



(a)



(b)

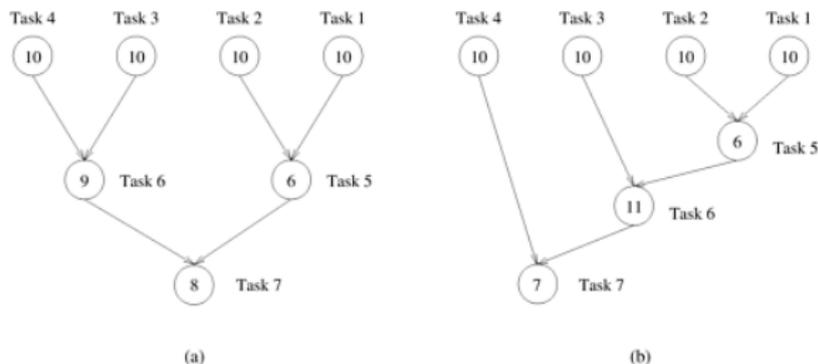
- ▶ Critical Path Length = Sum of longest path
- ▶ Maximum Degree of Concurrency = # of task in "widest" section
- ▶ Average Degree of Concurrency =

$$\frac{\text{Sum of all vertices}}{\text{Critical Path Length}}$$

# Computing Features of Dependency Graphs

## Maximum Degree of Concurrency

- ▶ (a) 4
- ▶ (b) 4



## Total Task Work

- ▶ (a) 63
- ▶ (b) 64

## Critical Path Length

- ▶ (a) 27 (leftmost path)
- ▶ (b) 34 (rightmost)

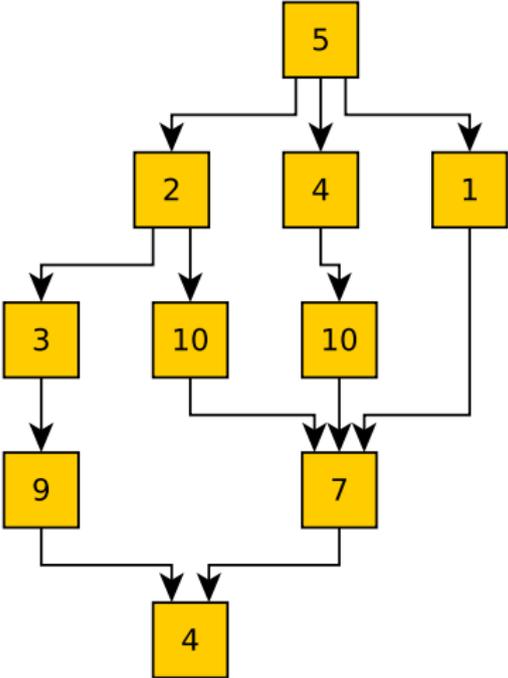
## Average Degree of Concurrency

- ▶ (a)  $63 / 27 = 2.33$
- ▶ (b)  $64 / 34 = 1.88$

# Exercise: Compute Features of Dependency Graph

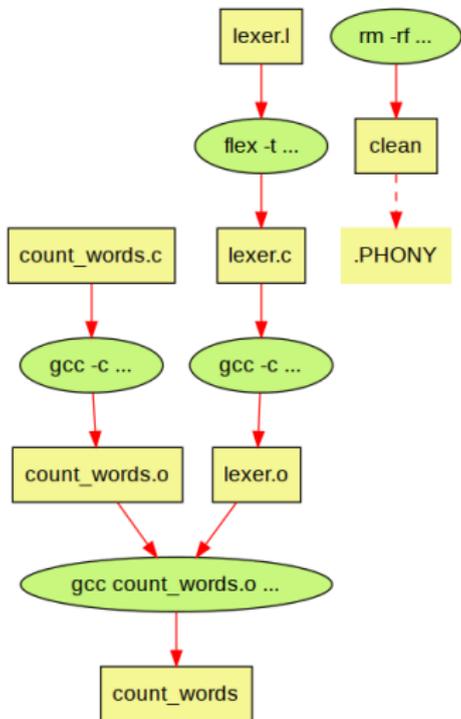
## Compute

- ▶ Total Work
- ▶ Maximum degree of concurrency
- ▶ Critical Path Length
- ▶ Average Degree of Concurrency



# Makefiles

- ▶ Most build systems for programs calculate task graphs
- ▶ Makefiles describe DAGs to build projects with make



Source: Luke Luo

```
count_words: count_words.o lexer.o
gcc count_words.o lexer.o -lfl \
-o count_words
```

```
count_words.o: count_words.c
gcc -c count_words.c
```

```
lexer.o: lexer.c
gcc -c lexer.c
```

```
lexer.c: lexer.l
flex -t lexer.l > lexer.c
```

```
.PHONY: clean
```

```
clean:
rm -rf *.o lexer.c count_words
```

Look up make `-j 4` option: use 4 processors for concurrency

# Identifying Tasks for Parallel Programs

- ▶ This is the tricky part
- ▶ Several techniques surveyed in the text that we'll overview
- ▶ Two general paradigms for creating parallel programs

## Parallelize a Serial Code

- ▶ Already have a solution to the problem
- ▶ Identify tasks within solution
- ▶ Construct a task graph and parallelize based on it
- ▶ We'll spend most of our time on this as it is more common

## Redesign for Parallelism

- ▶ Best serial code may not parallelize well
- ▶ Change the approach entirely to exploit parallelism
- ▶ Usually harder, more special purpose, spend less time on it

# Recursion Provides Parallelism

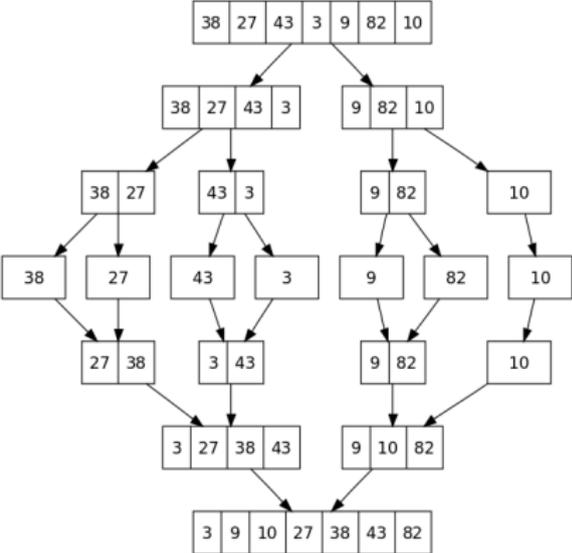
Algorithms which use *multiple* recursive calls provide easy opportunities for parallelism

## Multiple Recursive Call Algs

- ▶ Fibonacci calculations
- ▶ Mergesort
- ▶ Quicksort
- ▶ Graph searches

All reasonable for parallelizing:  
recursive calls are independent,  
represent independent tasks  
which can be run in parallel:

**parallelize a serial alg**



Source: Wikipedia Mergesort

# Reformulation As Recursive Algorithms

- ▶ Can sometimes reformulate an iterative algorithm as a recursive one:

Redesign for parallelism

- ▶ Show task graph for RECURSIVE\_MIN on array

$A = \{4, 9, 1, 7, 8, 11, 2, 12\}$

$n = 8$

```
procedure SERIAL_MIN (A, n)
begin
min = A[0];
for i := 1 to n - 1 do
    if (A[i] < min) then
        min := A[i];
    endif
endfor;
return min;
end SERIAL_MIN
```

```
procedure RECURSIVE_MIN (A, n)
begin
if (n = 1) then
    min := A[0];
else
    lmin := RECURSIVE_MIN (A, n/2);
    rmin := RECURSIVE_MIN (&(A[n/2]),
                            n - n/2);
    if (lmin < rmin) then
        min := lmin;
    else
        min := rmin;
    endelse;
endelse;
return min;
end RECURSIVE_MIN
```

# Data Decomposition: this is the big one

## Output Partitioning

- ▶ Collection of output data
- ▶ Tasks to compute output data are (relatively) independent
- ▶ Parallelize by assigning tasks based on output

## Input Partitioning

- ▶ Output tasks not easily independent
- ▶ Can build up output via independent tasks on input
- ▶ Requires a way to combine results from different sections of input
- ▶ Parallelize by assigning tasks to chunks of input then combining

- ▶ Combinations of Input/Output partitioning are common
- ▶ Examples to follow

# Matrix-Vector Multiplication

- ▶ Input: matrix A, vector x
- ▶ Output: vector b

$$A * x = b$$

$$\begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} ax + by + cz \\ dx + ey + fz \\ gx + hy + iz \end{bmatrix}$$

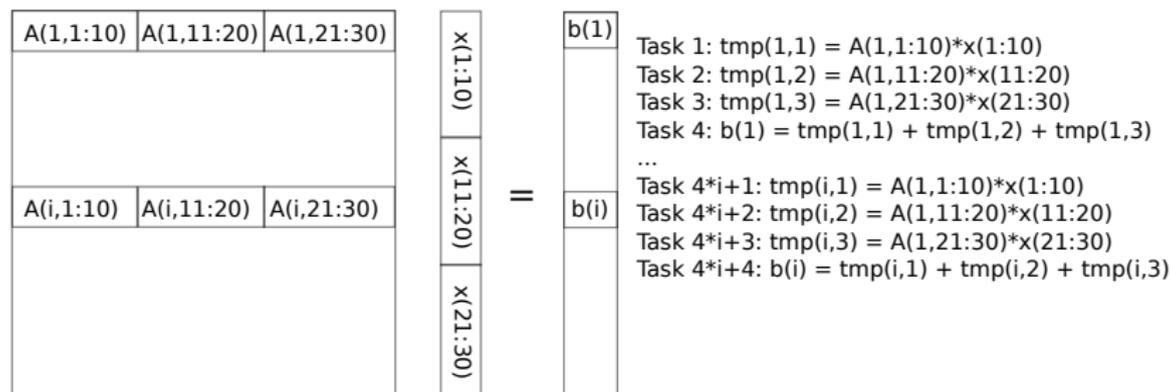
## Output Partitioning

- ▶ Task to compute each element of output b
- ▶ Each processor hold rows of A and all of x

## Input Partitioning

- ▶ **Constraint:** Processors have little memory, can't hold whole rows of A and all of x
- ▶ **Discuss** an input partitioning: chunks of A and x, do some computation, combine results to form elements of b

# Input Partitioning for Matrix-Vector Multiplication



- ▶ Most Tasks: multiply part of a row of A with part of x
- ▶ Some Tasks: combine partial sums to produce single element of output b

## Exercise: Frequent Item Set Calculation

Typical data mining task: count how many times items {D, E} were bought together in a database of transactions

- ▶ Input: database + itemsets of interest
- ▶ Output: frequency of itemsets of interest

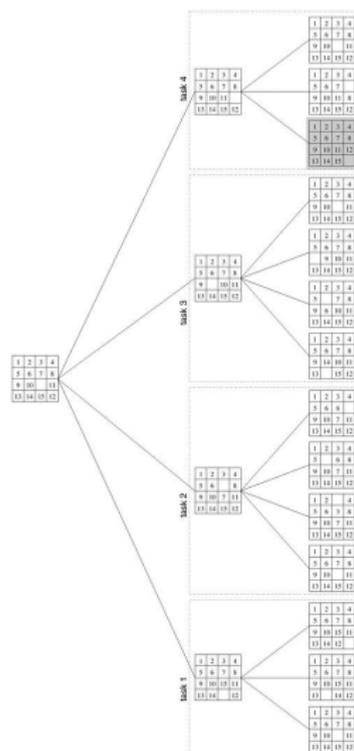
Describe tasks for...

- ▶ Input partitioning
- ▶ Output partitioning
- ▶ Combined partitioning

Database Transactions	A, B, C, E, G, H	Itemsets	A, B, C	Itemset Frequency	1
	B, D, E, F, K, L		D, E		3
	A, B, F, H, L		C, F, G		0
	D, E, F, H		A, E		2
	F, G, H, K,		C, D		1
	A, E, F, K, L		D, K		2
	B, C, D, G, H, L		B, C, F		0
	G, H, L		C, D, K		0
	D, E, F, K, L				
	F, G, H, L				

Answers in Grama 3.2

# Exploratory Decomposition



## Problem Formulations

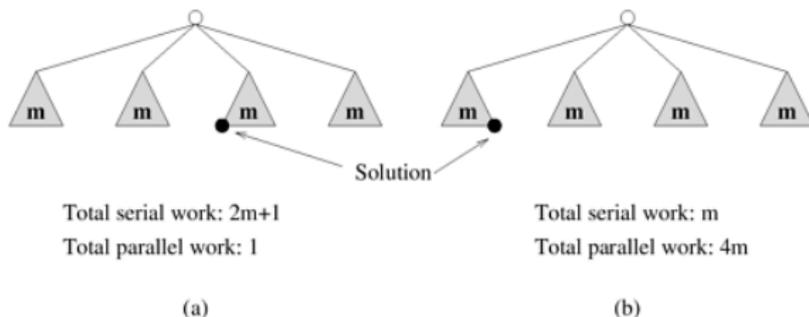
- ▶ Graph Breadth-first and depth-first search
- ▶ Path finding in discrete environments
- ▶ Combinatorial search (15-puzzle)
- ▶ Find a good move in a game (Chess, Go)

## Algorithms

- ▶ Similar to recursive decomposition
- ▶ Each step has several possibilities to explore
- ▶ Serial algorithm must try one, then unwind
- ▶ Parallel algorithm may explore multiple paths simultaneously

## Features of Exploratory Decomposition

- ▶ Data duplication may be necessary so each PE can change its own data (puzzle)
- ▶ Redundancy may occur: two PEs arrive at the same puzzle state
  - ▶ Detect duplication requires programming/communication
  - ▶ Ignoring duplication wastes PE time
- ▶ Termination is trickier: once a solution is found, must signal to all active PEs that they can quite or move on
- ▶ Can lead to strange "super-linear" speedups over serial algorithms or to much wasted effort



# Static and Dynamic Task Generation

## Static Task Generation

- ▶ All tasks known ahead of time
- ▶ Easier to plan and distribute data
- ▶ Examples abound: matrix operations, sorting (mostly), data analysis, image processing

## Dynamic task Generation

- ▶ Tasks are "discovered" during the program run
- ▶ Tougher to deal with scheduling, data distribution, coordination
- ▶ Difficulty with message passing paradigm
- ▶ Examples: game tree search, some recursive algorithms, others(?)

## Focus on Static Task Generation

## Static and Dynamic Scheduling (Mapping)

- ▶ Given tasks and dependencies, must schedule them to run on actual processors
- ▶ Problems to solve include Load imbalance (unequal work), Communication overhead, Data distribution as work changes

### Static Mapping/Scheduling

- ▶ Specify which tasks happen on which processes ahead of time
- ▶ Usually baked into the code/algorithm
- ▶ Works well for message passing/distributed paradigm

### Dynamic Mapping/Scheduling

- ▶ Figure out where tasks get run as you go
- ▶ More or less required if tasks are "discovered"
- ▶ Centralized scheduling Schemes: manager tracks tasks in a data structure, doles out to workers
- ▶ Distributed scheduling schemes: workers share tasks directly

# Reducing the Overhead of Parallelism

Parallel algorithms always introduce overhead: work that doesn't exist in a serial computation. Reducing overhead usually comes in three flavors.

1. Make tasks as independent as possible
2. Minimize data transfers
3. Overlap communication with computation

#1 and #2 are often in tension: **why?**

# Broad Categories of Parallel Program Designs

## Data-parallel

Every processors gets data, computes similar things, syncs data with group, repeats;  
Example: matrix multiplication

## Task Graph

Every processor gets some tasks and associated data, computes then syncs, Example: parallel quicksort (later)

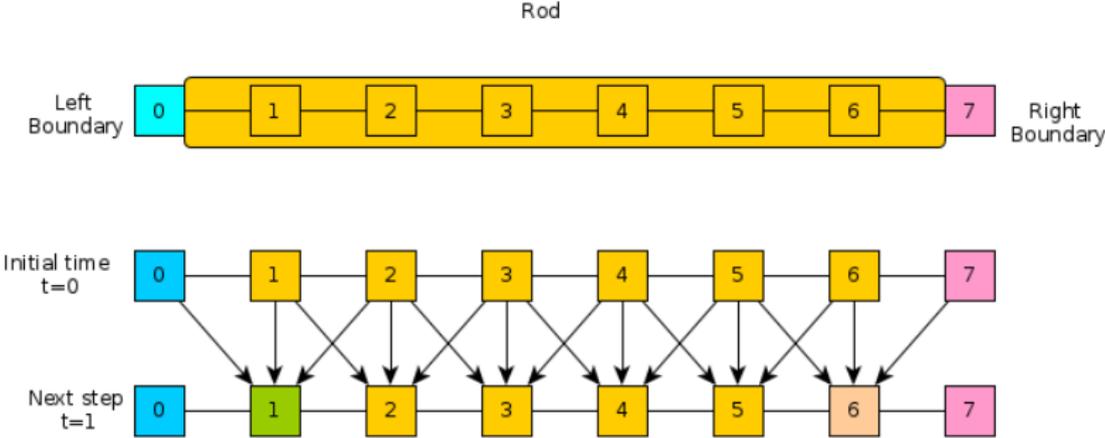
## Work-pool and Manager/Workers

Initial tasks go into pool, doled out to workers, discover new tasks, go into pool, distributed to workers. . . . Example: web server

## Stream / Pipeline / Map-Reduce

Raw data goes in, comp1 done to it, fed to comp2, then to comp3, etc. Example: Frequency counts of all documents, LU factorization

# Exercise: HW1's Heat Problem



- ▶ What are the tasks? How does the task graph look?
- ▶ What kind of scheduling seems like it will work?
- ▶ How should the data be distributed?
- ▶ What broad category of approach seems to fit?  
Data parallel, Task graph distribution,  
Work-pool/Manager-worker, Stream/Pipeline