

# CS 211

## RECURSION




# Recursion

A screenshot of a Google search page. The search bar contains the word "recursion". Below the search bar, the text "Search" is followed by a small profile picture and the text "7 personal results. 9,030,000 other results (0.27 seconds)". A yellow oval highlights a suggestion: "Did you mean: [recursion](#)". Below this, the first search result is for "Recursion - wikipedia, the free encyclopedia" with the URL "en.wikipedia.org/wiki/Recursion". The snippet for this result reads: "Recursion is the process of repeating items in a self-similar way. For instance, when the surfaces of two mirrors are exactly parallel with each other the nested ...". Below this is a link to "Formal definitions of recursion - Recursion in language". The second search result is for "Recursion (computer science) - Wikipedia, the free encyclopedia" with the URL "en.wikipedia.org/wiki/Recursion\_(computer\_science)". The snippet for this result reads: "Recursion in computer science is a method where the solution to a problem depends on".

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Google recursion

Search  7 personal results. 9,030,000 other results (0.27 seconds)

Everything **Did you mean: [recursion](#)**

Images **Recursion - wikipedia, the free encyclopedia**  
[en.wikipedia.org/wiki/Recursion](https://en.wikipedia.org/wiki/Recursion)  
Recursion is the process of repeating items in a self-similar way. For instance, when the surfaces of two mirrors are exactly parallel with each other the nested ...  
↳ [Formal definitions of recursion - Recursion in language](#)

Maps

Videos

News

Shopping **Recursion (computer science) - Wikipedia, the free encyclopedia**  
[en.wikipedia.org/wiki/Recursion\\_\(computer\\_science\)](https://en.wikipedia.org/wiki/Recursion_(computer_science))  
Recursion in computer science is a method where the solution to a problem depends on

More



# What is **Recursion**?

- Recursion generally means that something is defined in terms of itself.
  - functions/methods can be recursive
    - if it calls itself
  - data can be recursive
    - if a class "has-a" field of its own type



# Method Recursion

- We can call a method inside its own body.
- The **recursive call** should logically solve a "smaller" problem
- We must have some way to stop, called a **base case**. (It should be checked *before* the recursive call!)  
→ otherwise, it's just like an infinite loop!



# Example: Factorial

- In mathematics, the factorial  $n!$  is defined as  $n! = n * (n-1) * \dots * 2 * 1$ . It is defined for all non-negative numbers, and  $0! = 1$ . Examples:

$$5! = 5 * 4 * 3 * 2 * 1 \quad 100! = 100 * 99 * 98 * \dots * 3 * 2 * 1$$

$$3! = 3 * 2 * 1 \quad 1! = 1 \quad 0! = 1$$

- The **Base Case** is when  $n=0$ : we immediately know the answer. No recursion is necessary.
- The **Recursive Case** is when  $n>0$ : we know that whatever value  $n$  has,  $(n-1)$  will be one step closer to the base case of  $n=0$ .
  - assume the method is already correct; phrase  $n! = n * (n-1)!$
  - call our method on  $(n-1)$ , and multiply it by  $n$ .
  - let the recursive call do the rest!

# Example: Factorial

```
public static int factorial (int n) {  
  
    //base case, no recursion  
    if (n==0) { return 1; }  
  
    //recursive case:  $n! = n*(n-1)!$   
    else {  
        int nfact = n * factorial(n-1);  
        return nfact;  
    }  
}
```



# Recursive Calls: Details

- When a method calls itself, each call is distinct (separate)
  - each separate call has its **own copy of local data**
  - for `factorial`, each call has its own value for parameter `n`.

Base Case Reached! Non-recursive call can complete.

factorial (0)	n 0	$0! == 1$
factorial (1)	n 1	$1! == 1 * 0! == 1$
factorial (2)	n 2	$2! == 2 * 1! == 2$
factorial (3)	n 3	$3! == 3 * 2! == 6$



# Recursion Recipe

- To use recursion, you might want to follow this pattern:
    1. Identify the base cases: times when you already know the answer
    2. Identify the recursive cases: times when you can define one step of the solution in terms of others
      - Is the recursive step using the method on a "smaller" problem? (needs to be yes!)
    3. Write code for the base case *first*
    4. Write code for the recursive case *second*
- handle any error conditions like base cases: e.g., factorial shouldn't be called on negative numbers, so choose how to exit meaningfully.



# Recursion Example: Fibonacci

- The fibonacci sequence looks like:

1, 1, 2, 3, 5, 8, 13, ...

- Its first two elements are each 1.
  - the  $n$ th element is the sum of the previous two elements.
- 
- We can number them like array slots:  
 $\text{fib}(0) == 1$ ,  $\text{fib}(6) == 13$ , etc.



# Practice Problems

Implement the fibonacci method, which accepts the 'index' number  $n$ , and then returns that fibonacci number.

Questions (suggested solution path):

- What are the base cases?
- What are the recursive cases?
- What are some good test cases?

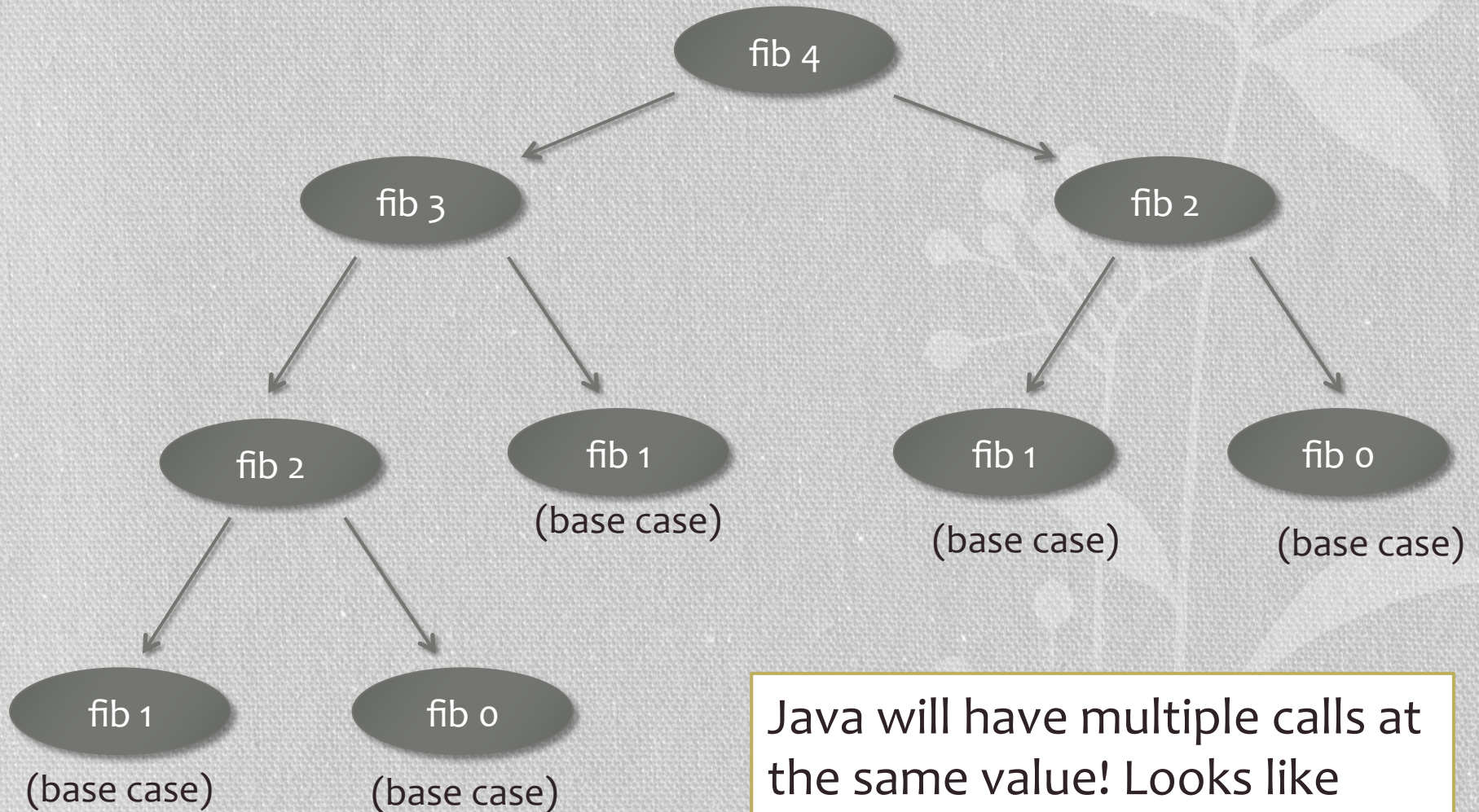


# Fibonacci Code

```
public static int fib (int n) {  
  
    // base cases  
    if (n==1 || n==0) { return 1; }  
  
    //recursive case  
    else {  
        return fib(n-1) + fib(n-2);  
    }  
}
```



# Visualizing Fibonacci Calls



Java will have multiple calls at the same value! Looks like wasted effort...



# Iterative Version of Fibonacci

```
public static int fibIter (int n) {  
    //base cases  
    if (n==1 || n==0) { return 1; }  
  
    //iterative cases  
    int lower = 1;  
    int higher = 1;  
    for (int i = 2; i <=n; i++ ) {  
        int temp = lower+higher;  
        lower = higher;  
        higher = temp;  
    }  
    return higher;  
}
```



# Considering Recursion

## Recursion: **Pros**

- Sometimes much easier to reason about
- distinct method calls help separate concerns (separate our local data per call).
- Easy to maintain separate state (values) each recursive call

## Recursion: **Cons**

- Sometimes, lots of work is duplicated (leading to quite long running time)
- Overhead of a method call is more than overhead of another loop iteration



# Considering Iteration

## Iteration: **Pros**

- quick, barebones.
- Simpler control flow (we perhaps see how iterations will follow each other easier than with recursion)
- no stack overflow errors

## Iteration: **Cons**

- some tasks do not lend well to iterative definitions (especially ones with lots of bookkeeping/state)
- We tend to be given mathematical, "recursive" definitions to problems, and then have to translate to an iterative version.



# Recursion versus Iteration

So, which one is better?

→ it depends on the situation.

- When might we prefer recursion?
- When might we prefer iteration?





# Practice Problems

What are some cases that might merit recursion?

Thinking experiment: How can you use recursion to...

→ check if a number is even?

→ find the log of a number? (return an int)

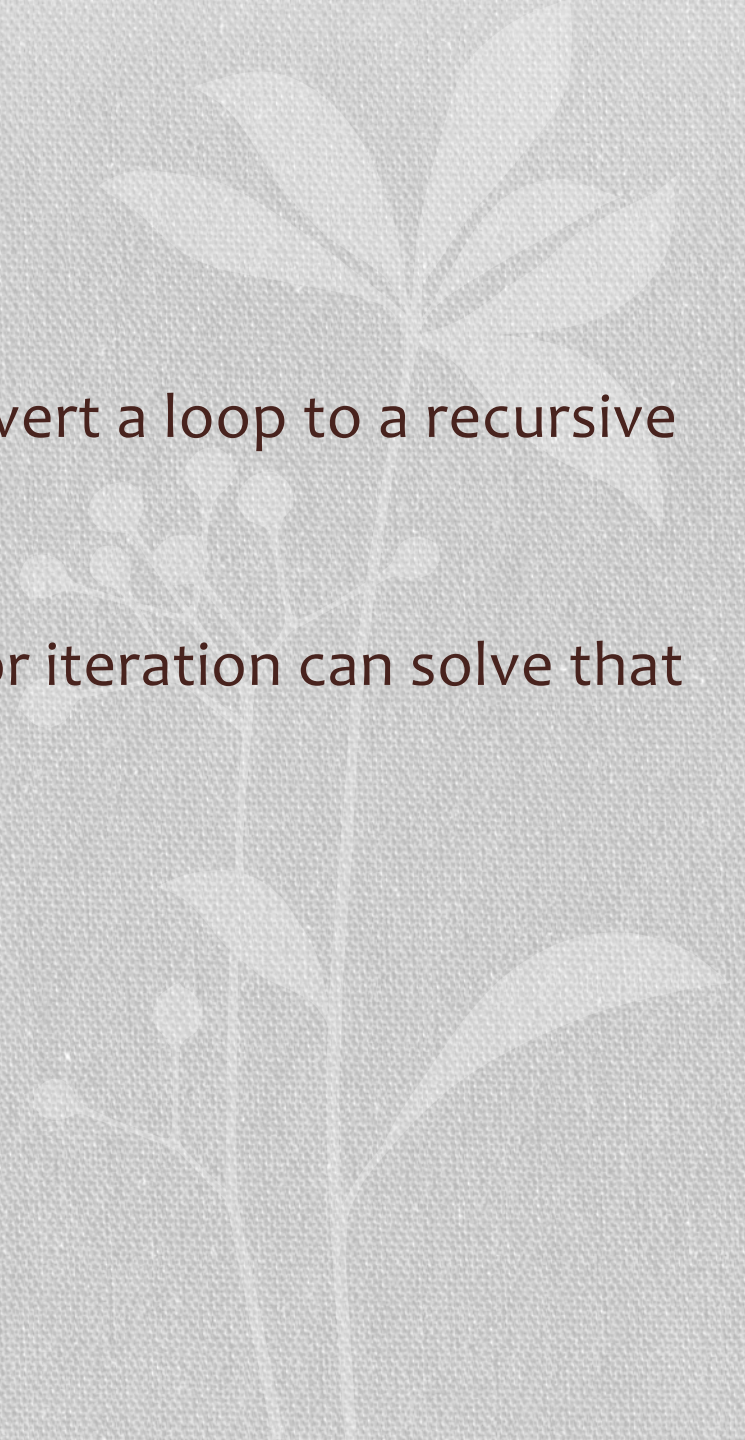
→ solve a maze?

→ solve a sudoku?



# Practice Problems

- How, in general, might we try to convert a loop to a recursive method call?
- Is there any problem that recursion or iteration can solve that we couldn't solve with the other?



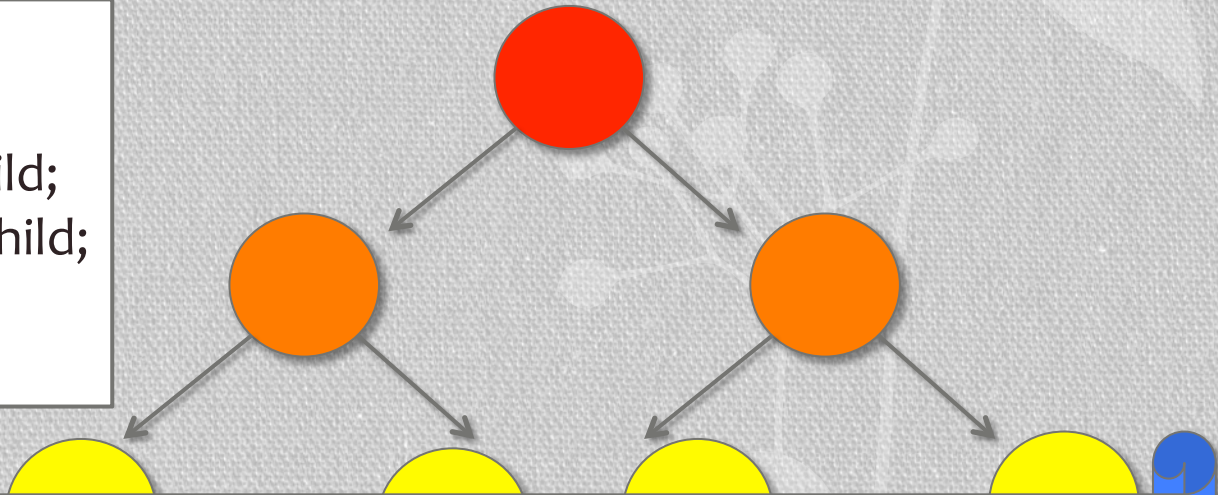


# Data Recursion

Data can also be recursive: when a class definition contains a field whose type is the same as the class being defined:

```
public class Tree {  
    public int value;  
    public Tree leftChild;  
    public Tree rightChild;  
    ...  
}
```

recursive fields

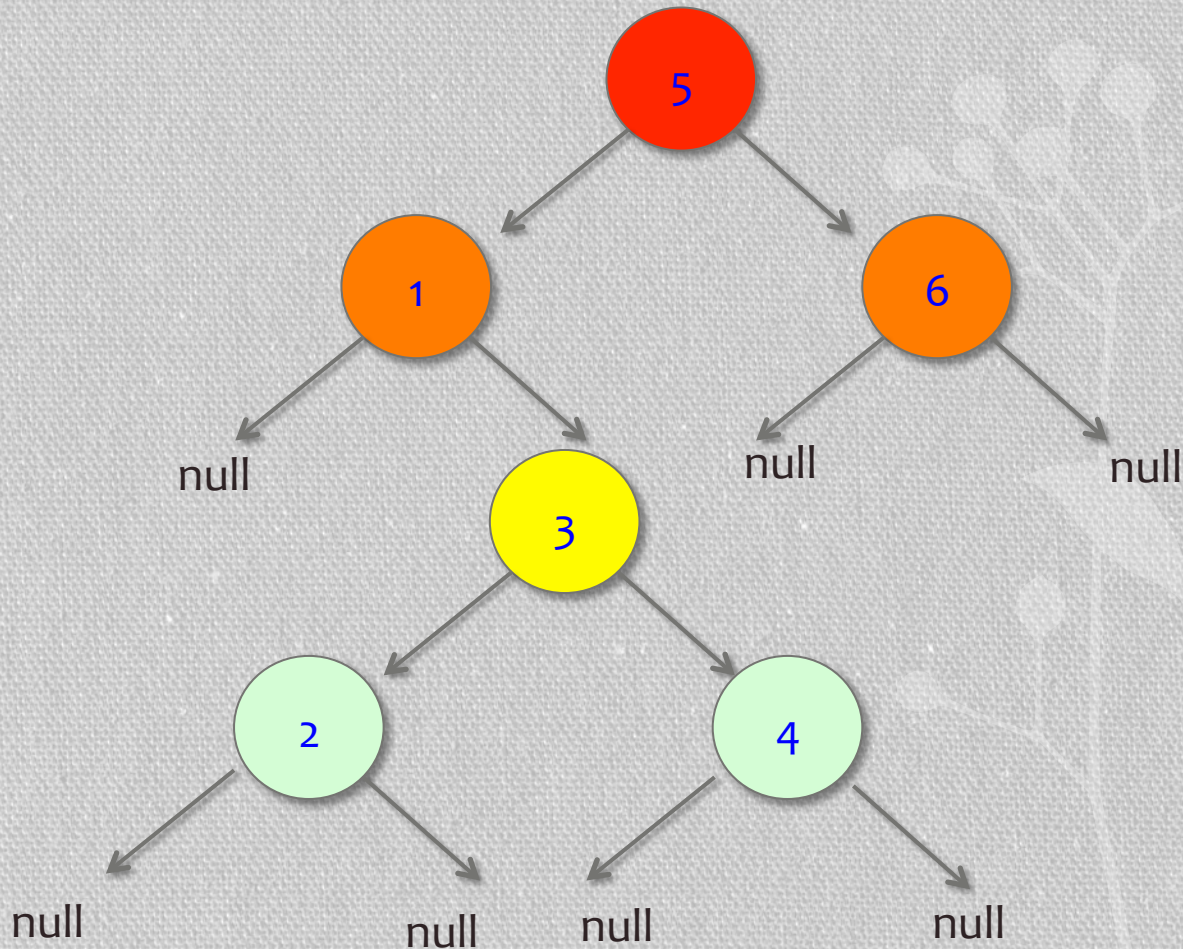


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..... How is this ever useful?!



# Base Cases in Data Recursion

- We will again end the recursion with a base case: the **null** value.

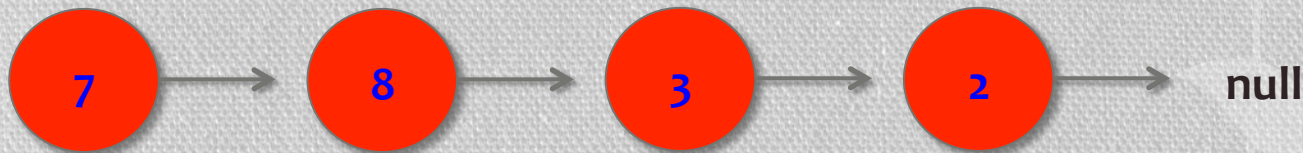




# Linked Lists

What if our `Tree` only had one branch? And we named it `IntList`?

```
public class IntList {  
    public int val;  
    public IntList next;  
    ...  
}
```



It looks a lot like the array `int[] xs = {7,8,3,2};`  
→ could we implement the usual operations over our `IntList` that are usually available on arrays?



# Making a Linked List Useful

- We might want to add these sorts of operations over our `IntList`:
  1. **size** (how many elements are in here?)
  2. **add a value** (sorted? always at the end?)
  3. **remove a value** (just tell us which value to remove)
  4. **check if a value is present** (return a boolean)
  5. **makeArrayVersion** (create an old-fashioned array out of it)
- We can approach these tasks thinking of the diagrams of "before" the operation, "after" the operation, and then write code that implements these changes. Now we're *\*really\** programming with our own data structures!



# More Data Structures

There are many common data structures. **CS 310** is a course entirely devoted to them! It. Is. Awesome.

Some others:

- Linear stuff → Lists, Stacks, Queues, ...
- Trees → binary, balanced, ...
- Graphs → networks, DiGraphs, ...
- Hashes → hashes



# Java Libraries for Data Structures

- We should take a look at the ArrayList class in Java:

go to: *(google "Java ArrayList")*

<http://docs.oracle.com/javase/1.5.0/docs/api/java/util/ArrayList.html>