Alpha-Beta Pruning Example



Problem #7

A partial search tree for a two player game is given below.

- a) Find the best move for the MAX player using the minimax procedure.
- b) Using alpha-beta pruning show which parts of the tree do not need to be searched. Indicate where the cutoffs occur.



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Problem #7: Minimax



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Problem #7: Alpha-beta Pruning



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Problem #22

Consider the following game tree.

- (a) Find the best move for the MAX player using the minimax procedure.
- (b) Perform a left-to-right alpha-beta pruning on the tree. Indicate where the cutoffs occur.
- (c) Perform a right-to-left alpha-beta pruning on the tree. Discuss why different pruning occurs.



Problem #22: Minimax



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Problem #22: Alpha-beta pruning left to right



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Problem #22: Alpha-beta pruning right to left



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Problem #30: A nim-game tree

A simple version of the *nim* game is played as follows: Two players alternate in removing stones from three piles initially containing two, two, and three stones, respectively. The player who picks up the last stone wins. At any given turn a player can pick one or more stones from a single pile; at least one stone has to be picked every time.

- a) Show, by drawing a game tree, which player can always win.
- b) Is it necessary to generate the whole tree to find a winning strategy? Explain why or why not.

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Problem #30: A nim-game tree solution



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